

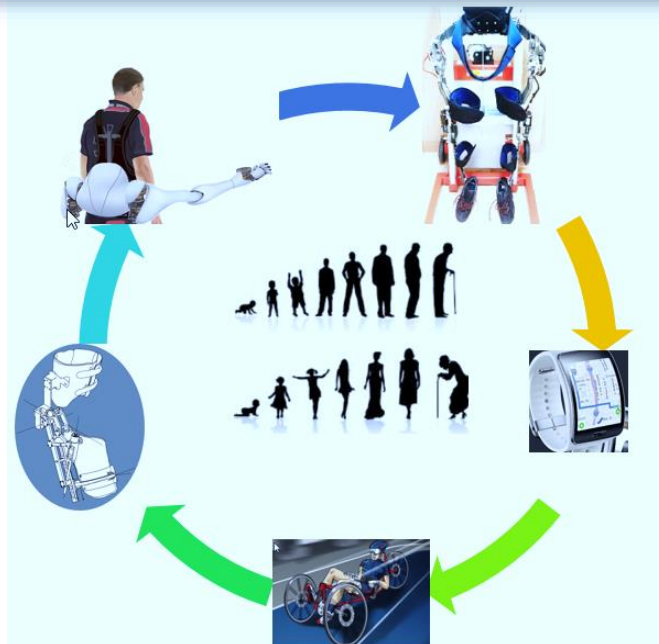
# An assistive MPC-Based Framework for a Robotic Knee Rehabilitation Exoskeleton

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# My research activities in Robot Control

lirmm



<http://www.lirmm.fr/~chemori>

- ❑ Introduction & Context
- ❑ Some basic definitions & Main applications
- ❑ A brief historical overview & Some examples of today
- ❑ Experimental setup: EICOSI Orthosis (@LISSI – UPEC)
- ❑ Proposed control solutions (L1 adaptive , MPC)
- ❑ Real-time experimental results
- ❑ Conclusion

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Brief history

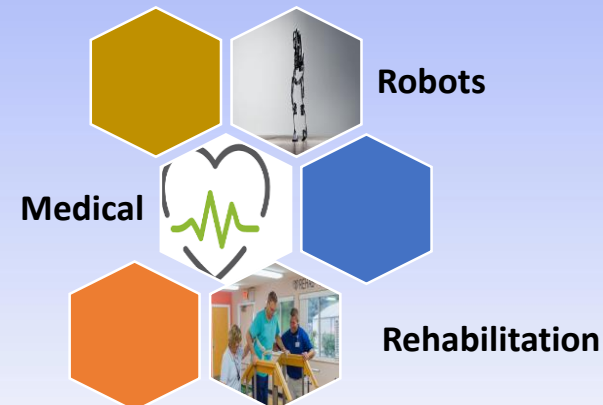
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# Introduction & Context





# Introduction & Context

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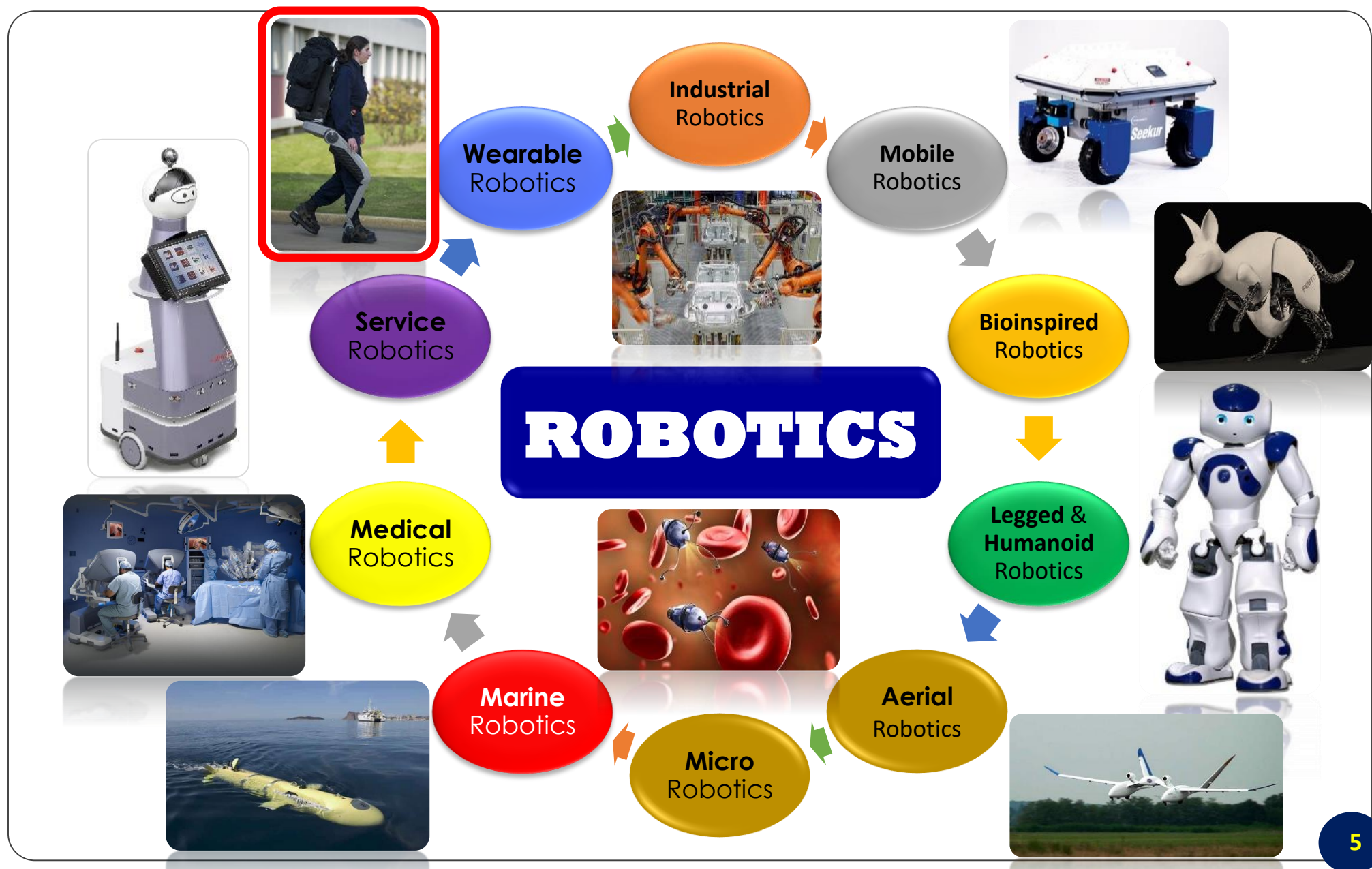
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Speaker : **A. CHEMORI**



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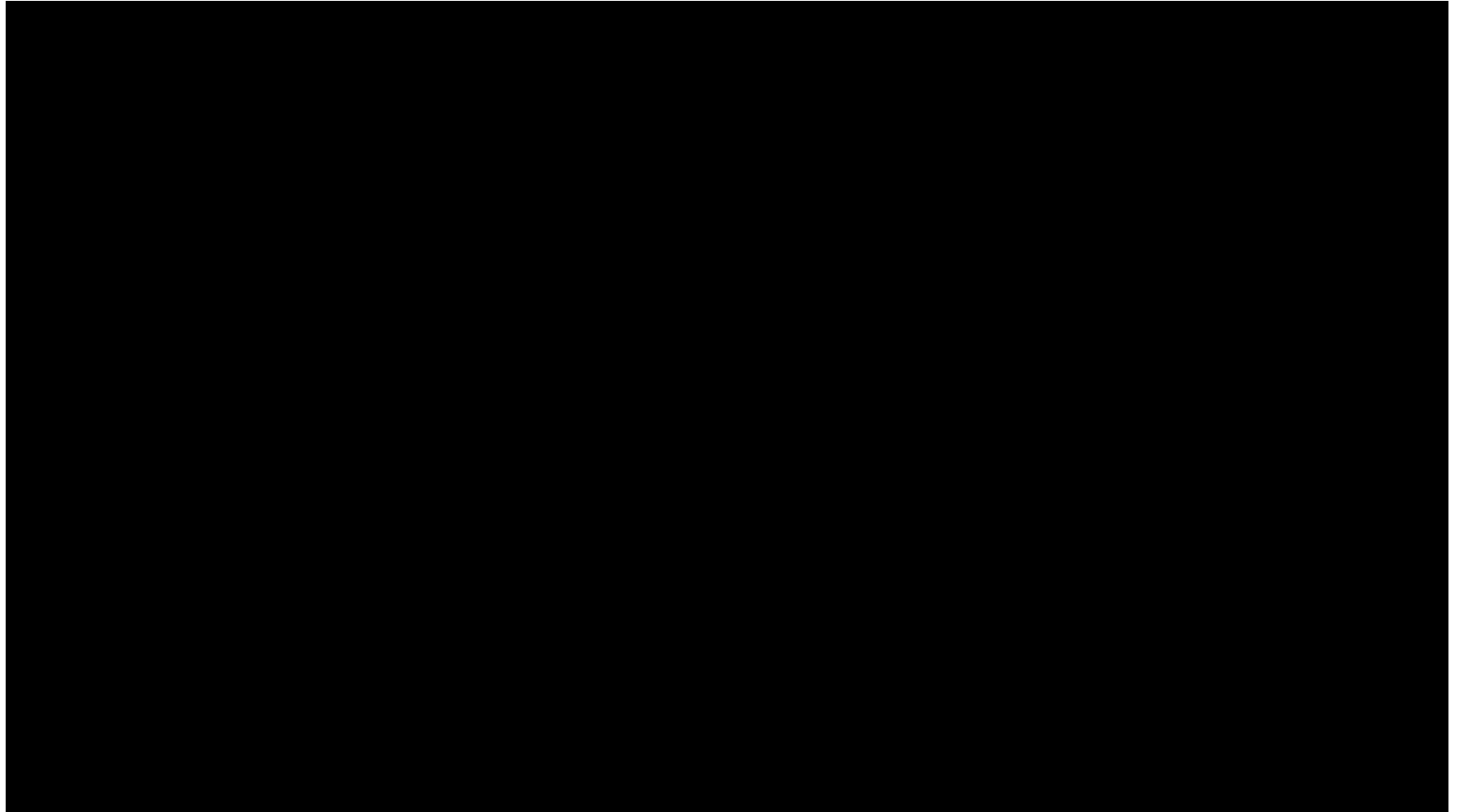
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# Introduction & Context

## Context

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How we can help them ?



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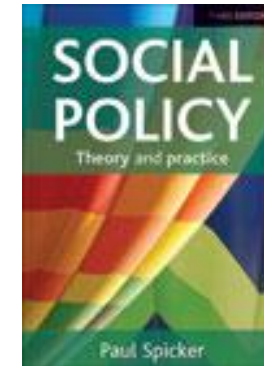
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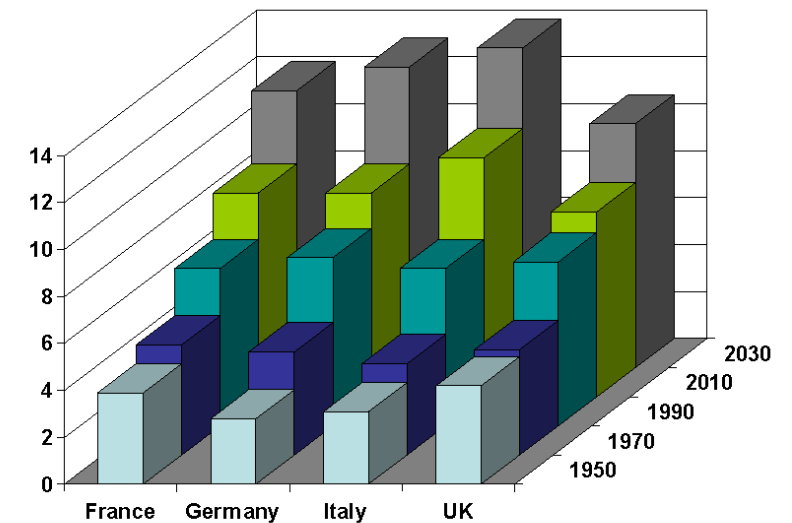
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By  
Paul Spicker

% of population over 65





## Context

## Definitions

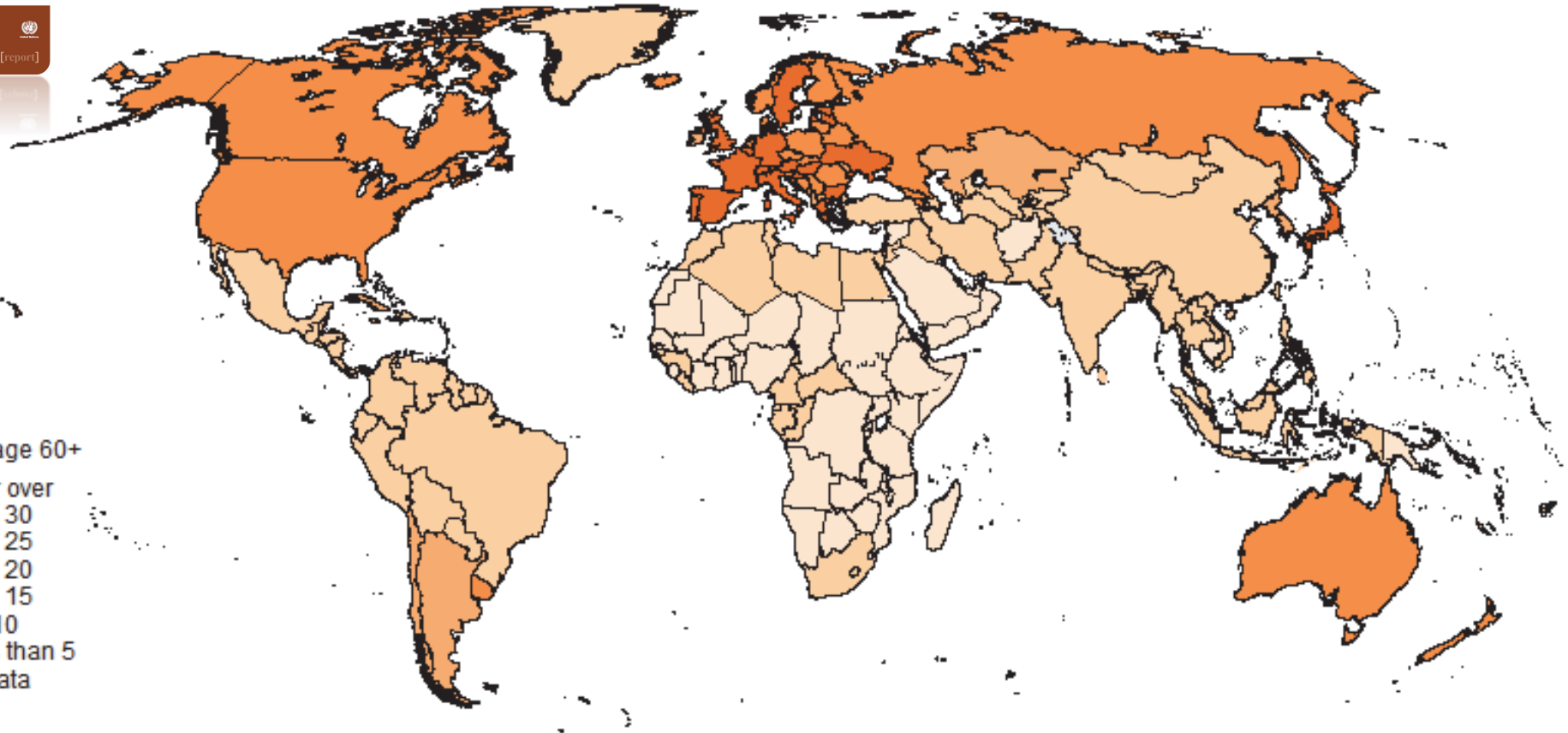
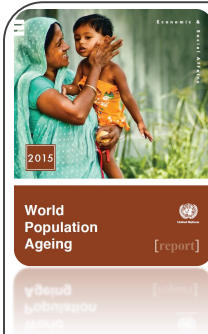
## Brief history

## Prototypes

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## Results

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Data source: United Nations (2015). World Population Prospects: The 2015 Revision

## Context

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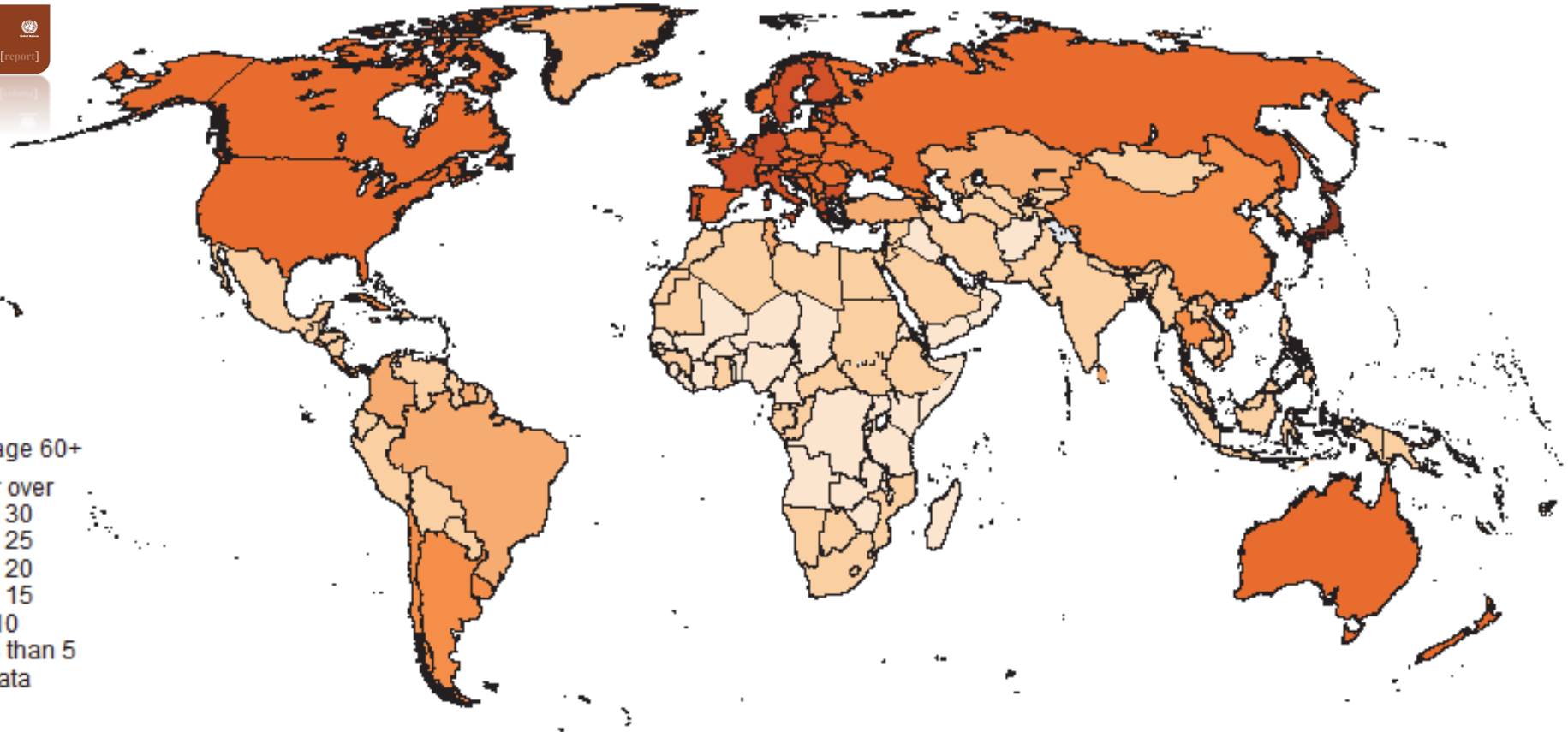
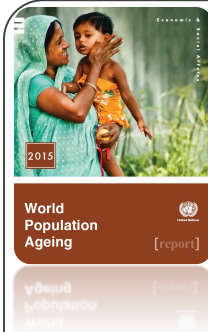
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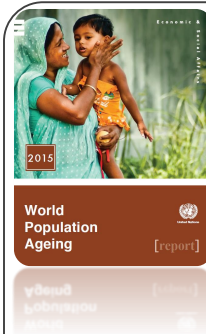
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Number of old people is rising faster than ever !

2050



Percentage 60+

- 30 or over
- 25 to 30
- 20 to 25
- 15 to 20
- 10 to 15
- 5 to 10
- Less than 5
- No data



What would be the solution to their mobility problems ?

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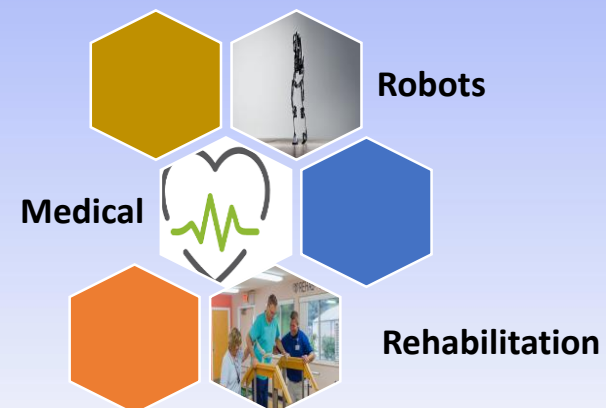
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# Some basic definitions





# What is an exoskeleton ?

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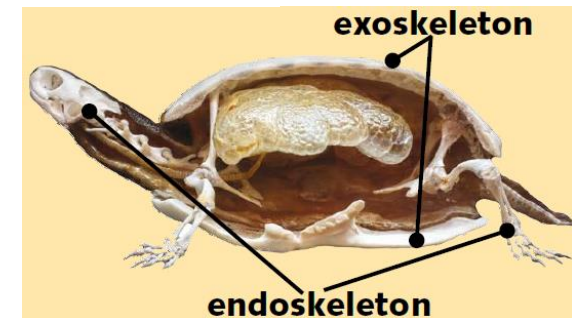
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- ✓ Animals and humans have **skeletons**
- ✓ To **protect** and support **inner working** of their bodies
- ✓ **Muscles** are attached to skeletons so be able to **move**
- ✓ Skeletons **inside** bodies are called **endoskeletons**
- ✓ Some animals have skeletons on the **outside** of their bodies, they are called **exoskeletons**
- ✓ Animals with exoskeletons live on land and in water,
- ✓ Include : **Crustaceans** and **insects**
- ✓ Like : **Spiders, shrimps, crabs**, etc
- ✓ Other animals have both **endo** and **exoskeletons** like turtles





# What is an exoskeleton ?

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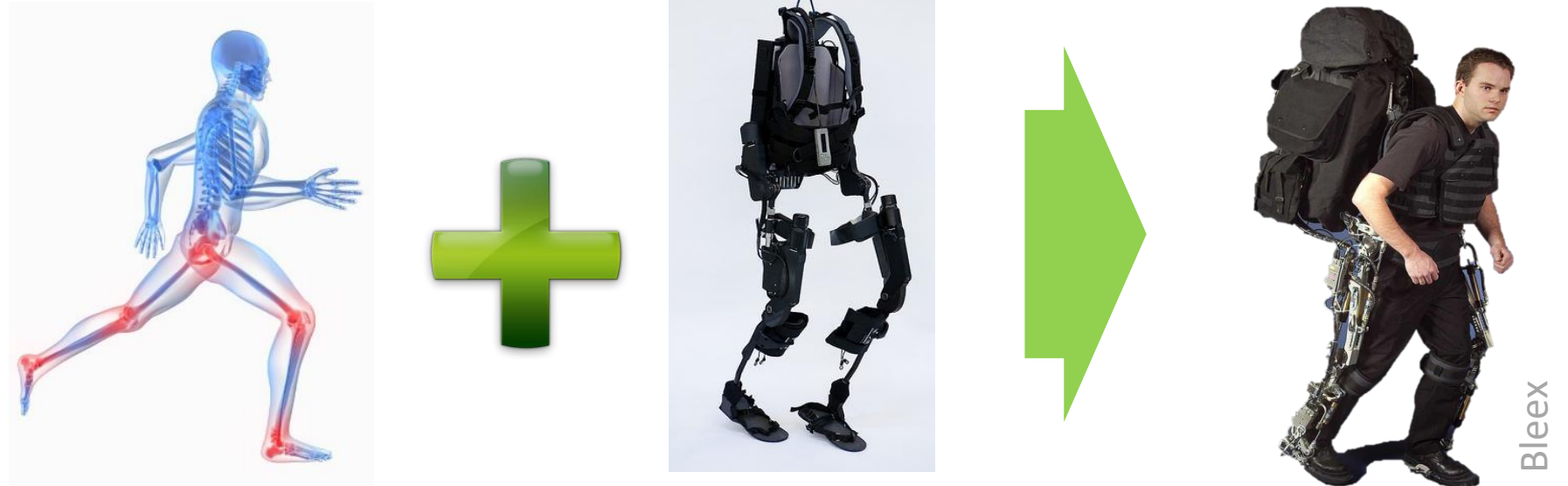
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- ✓ It is a **mechanical frame** designed to be **worn by a human being**
- ✓ **Designed** around the **function** and **shape** of the **human body**



- ✓ It **moves** with the **wearer**, adding **strength** and **durability**
- ✓ **Additional** strength/protection/support, benefit people in **dangerous/tiring jobs** or **mobility** issues
- ✓ Developed **initially** for **military** applications

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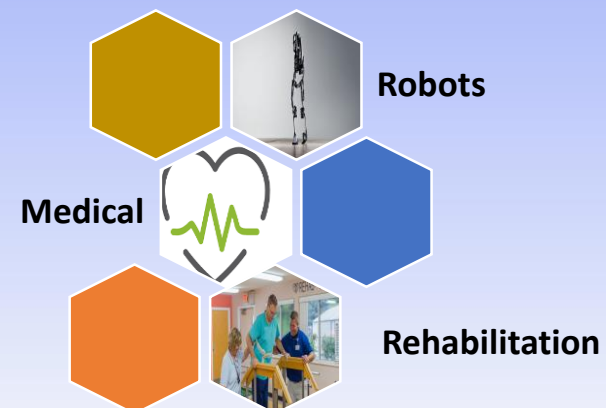
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# Main Applications



# Where exoskeletons are used ?

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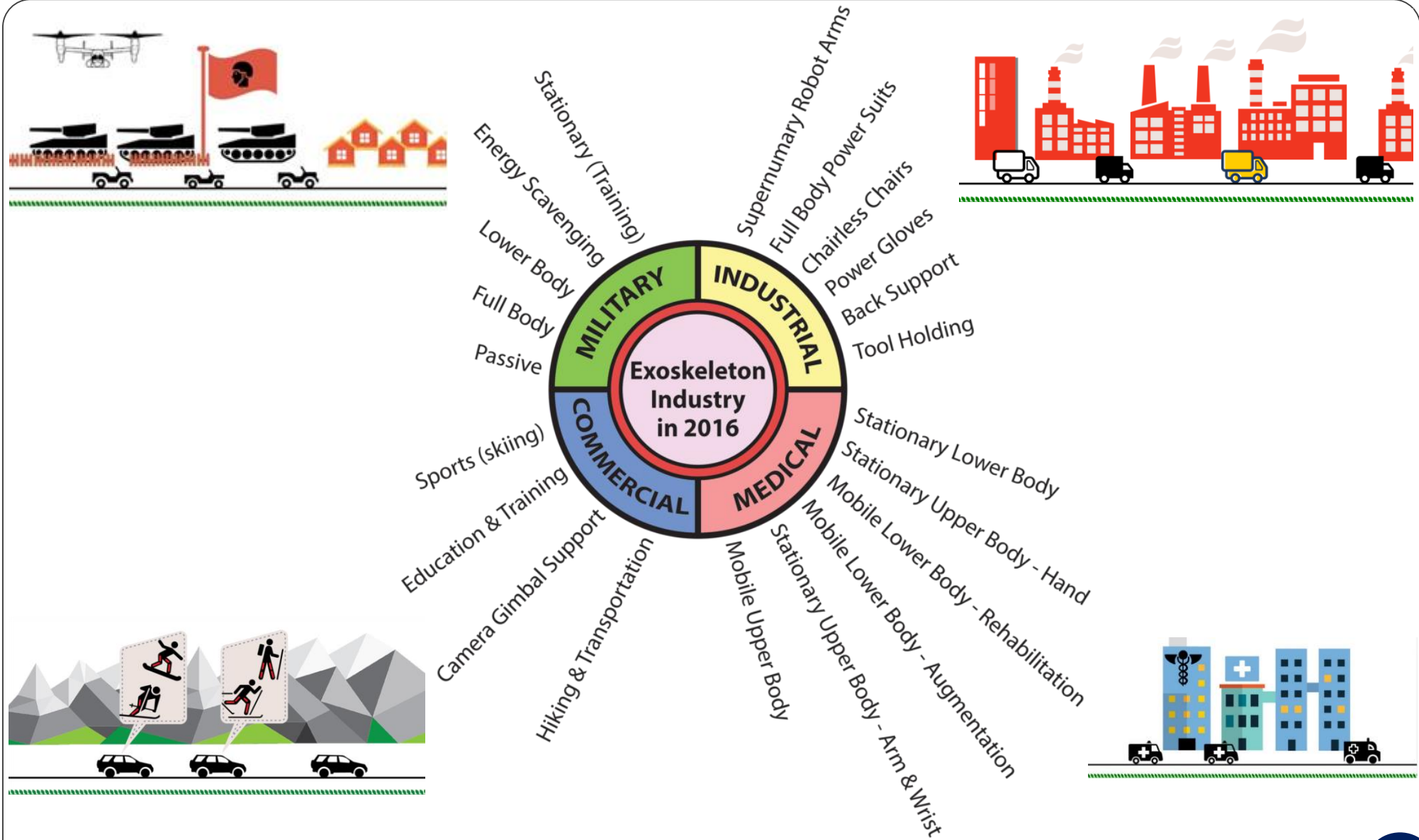
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Source : <https://exoskeletonreport.com/2016/08/exoskeleton-industry-2016/>



# Where exoskeletons are used ?

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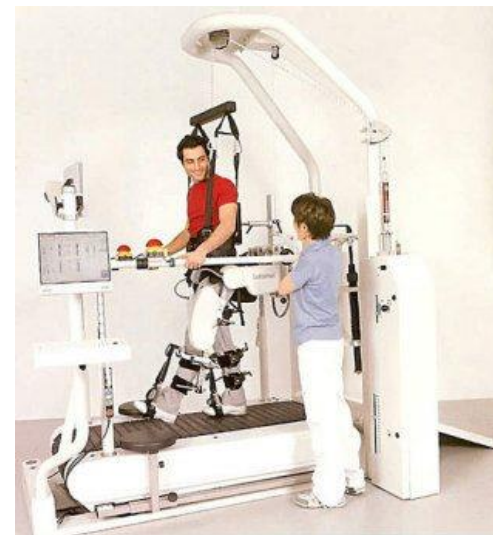
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Speaker : **A. CHEMORI**

**Medical applications** : Assistive devices in physical therapy (rehabilitation), amplify muscles' strenght, restore locomotion to paralyzed persons, stroke, spinal cord injury, etc.



# Where exoskeletons are used ?

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**Consumer/Civilian applications :** Assist humans in daily life tasks and also elderly persons (balance, carry loads, site to stand, etc)



HAL Exoskeleton



Ekso Bionics Exoskeleton



PANASONIC Exoskeleton



# Where exoskeletons are used ?

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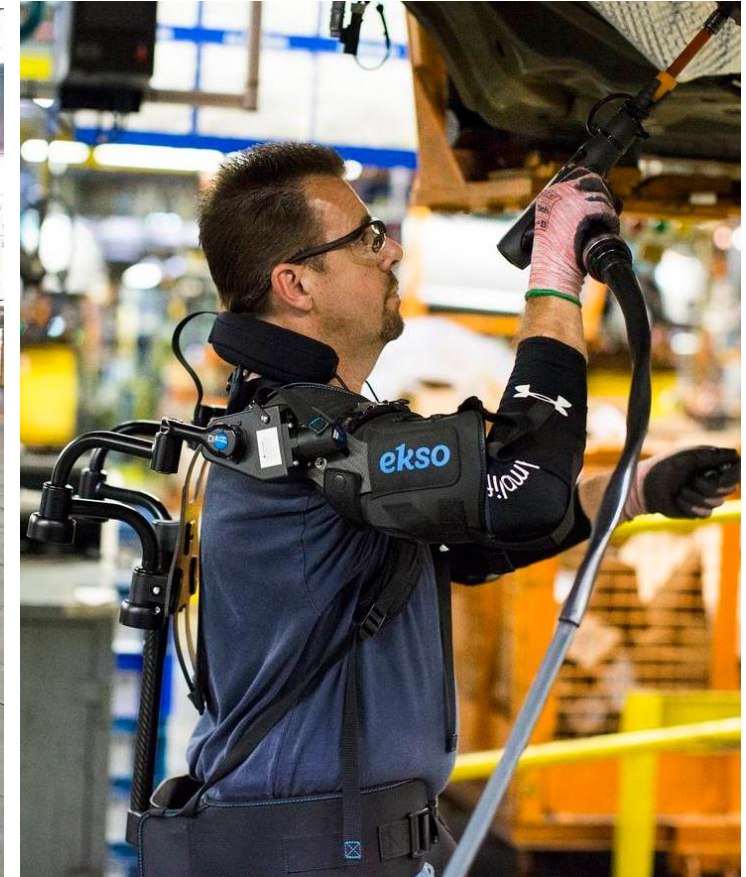
**Work/Industry applications** : To ease physical exertion in industry (force multiplier, Distributes weight to reduce user strain, reduce fatigue, etc)



FORTIS Exoskeleton



DAEWOO Exoskeleton



FORD Exoskeleton



# Where exoskeletons are used ?

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**Military applications** : To enhance soldiers' ability, protect soldiers, amplify strength, increase endurance, improve efficiency, etc



HULC, EKSO BIONICS



XOS 2, SARGOS/RAYTHEON

# Where exoskeletons are used ?

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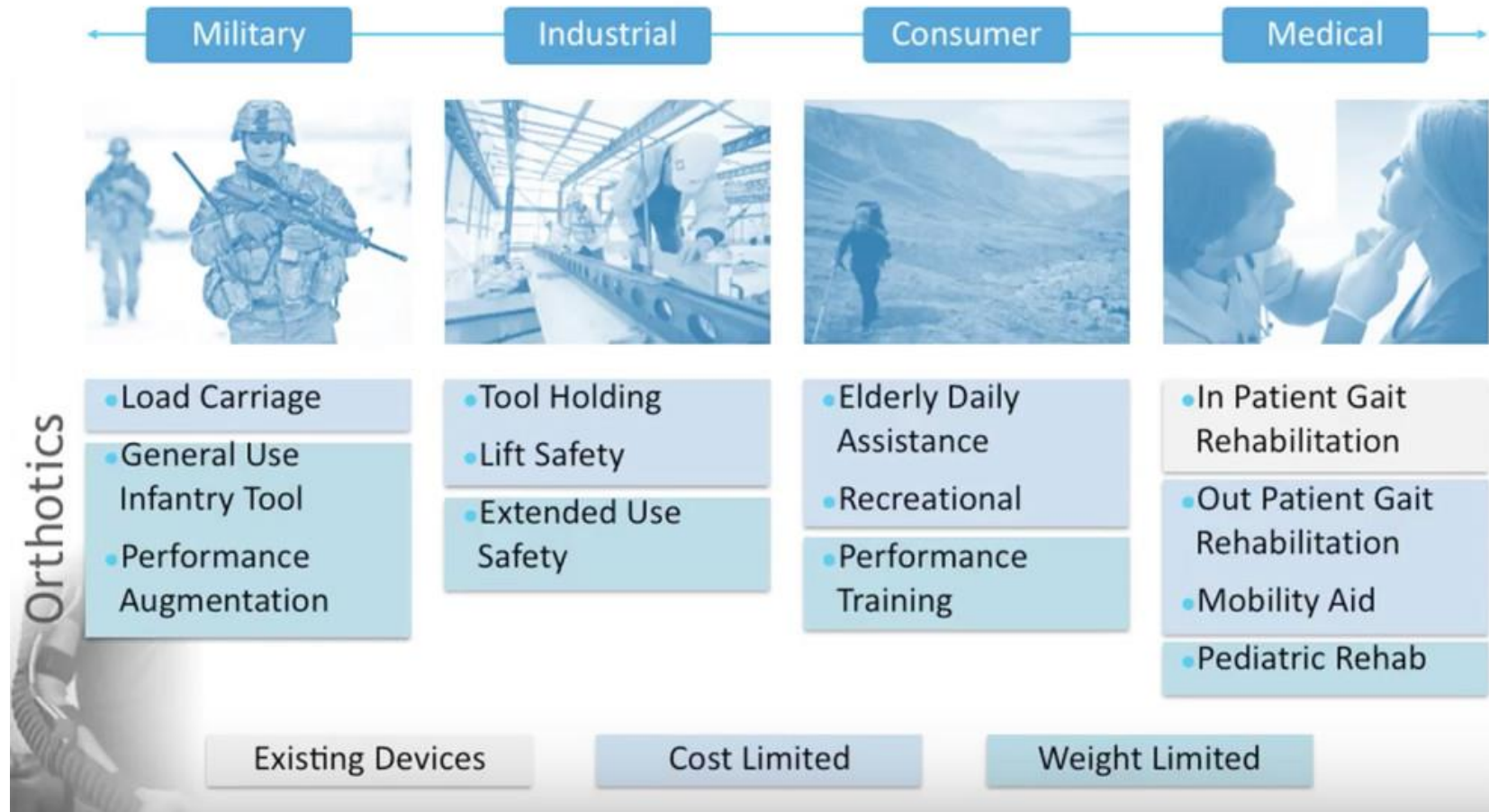
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## Addressable Markets





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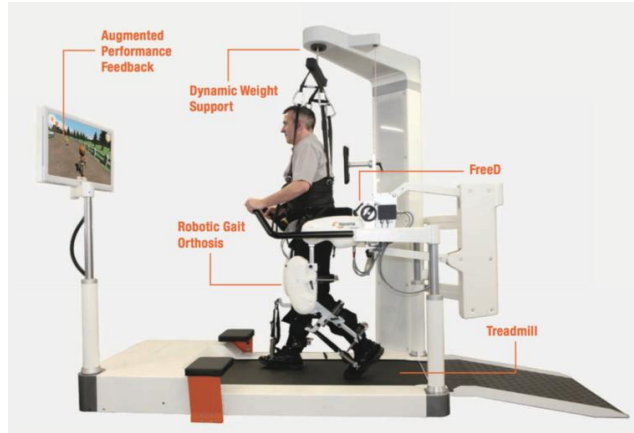
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Stationary vs mobile / Lower body vs upper body

Lower body

Stationary



Hocoma – Lokomat

Mobile

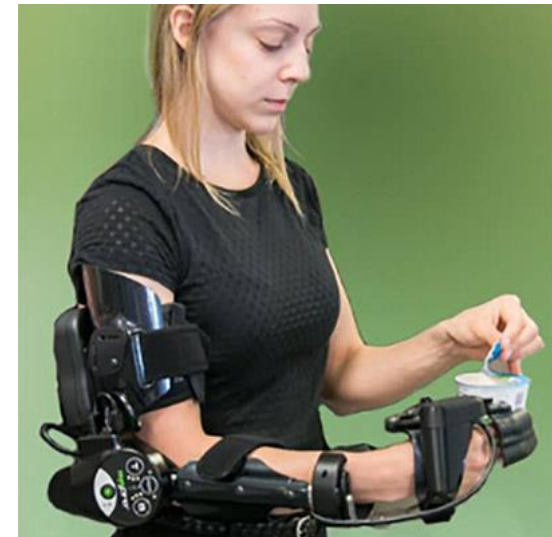


HANK by Gogo

Upper body



InMotion Arm, Bionik Lab



MyoPro by Myomo

# Control framework

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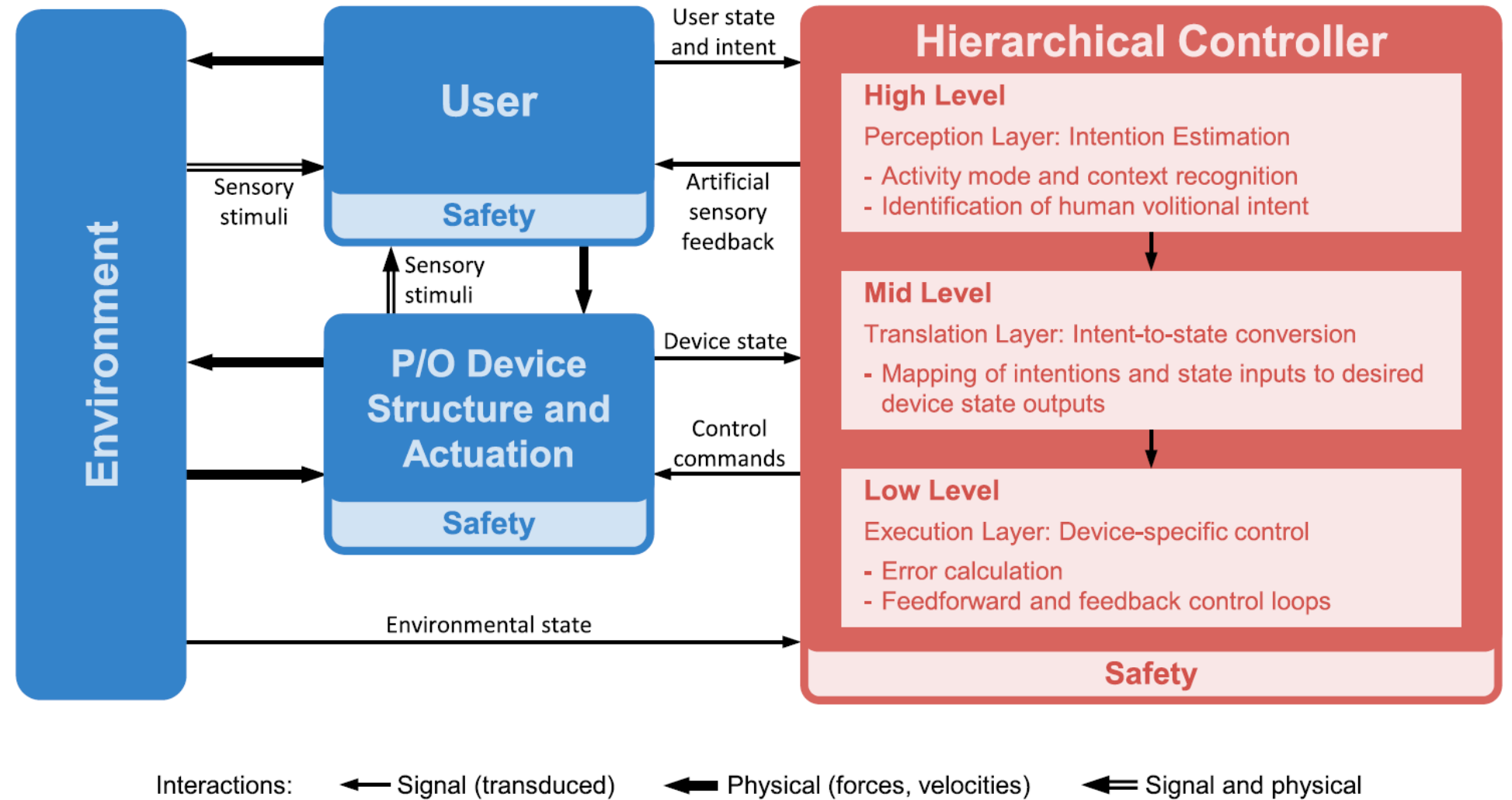
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[Ticker et al. 2015]



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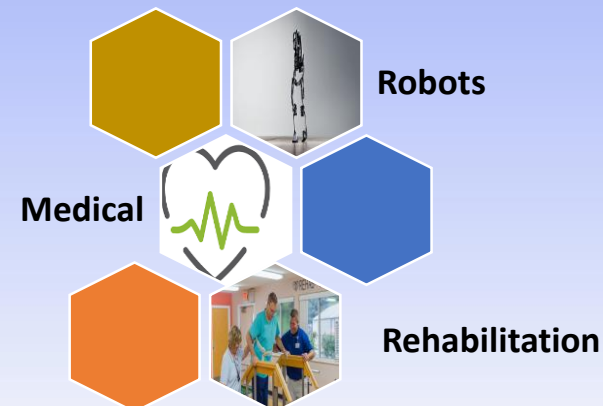
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# A brief historical overview



# A brief historical overview

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**Brief history**

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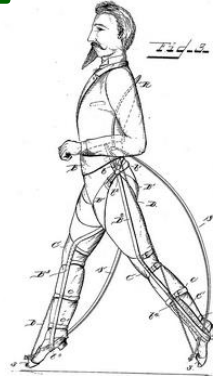
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## Brief historical overview

### Yagn's running aid

1890



- ✓ Never build
- ✓ Concept studies drawing
- ✓ Simple bow/leaf-Spring

### Hardiman

1960's



- ✓ 680 kg, 30 DOFs
- ✓ Full-body hydraulically powered
- ✓ Amplify drastically human force

### Mihailo Pupin

1971



- ✓ Pneumatic actuators
- ✓ Flex/Ext : hip, knee, and ankle
- ✓ Abduction/adduction : hip

### Berkley Bleex

2004



- ✓ 7dof/leg : 3dofs/hip, 1dof/knee, and 3dofs/ankle
- ✓ First "load-bearing and energetically autonomous"
- ✓ 4 dof actuated (2 hip, 1knee, 1 ankle)
- ✓ Linear hydraulic actuators

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## Brief historical overview

### Sarcos XOS suit

**2006**



- ✓ For military applications
- ✓ 25x strength amplification, Still tethered
- ✓ weighs 68 kg and allows lifting 90 kg

### Rewalk

**2011**



- ✓ For disabled people
- ✓ Light wearable brace support suit
- ✓ DC motors at the joints, rechargeable batteries
- ✓ Physiological and psychological benefits

### HAL 5

**2012**



- ✓ Designed to support and expand the physical capabilities of its users
- ✓ For people with physical disabilities
- ✓ Allow carrying loads
- ✓ Weight only 10 Kg



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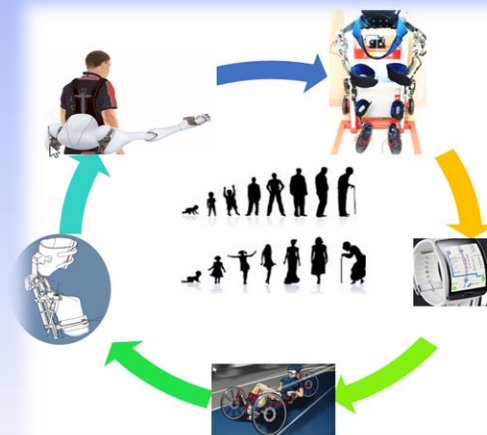
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# Some examples of exoskeletons



# 10 examples of exoskeletons

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# Examples of commercialized exoskeletons

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<http://exoskeletonreport.com/2015/04/12-commercial-exoskeletons-in-2015/>



# Examples of commercialized exoskeletons

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1 ReWalk



2 Ekso



3 Indego



4 REX

# Examples of commercialized exoskeletons

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5 Lokomat



6 HAL



7 Walking Assist



8 Hercule



# Examples of commercialized exoskeletons

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9 DSME



10 Exoatlet



11 FORTIS



12 AGAINER



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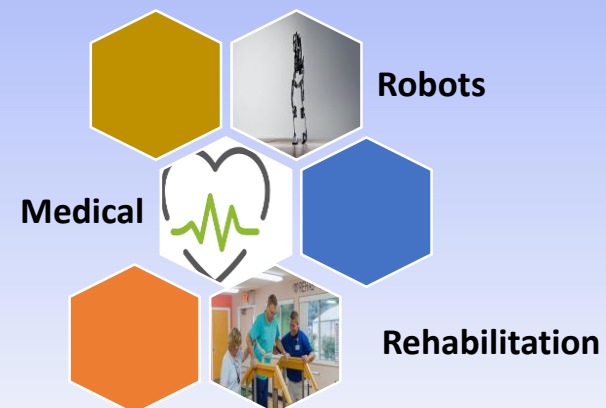
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# Our experimental setups



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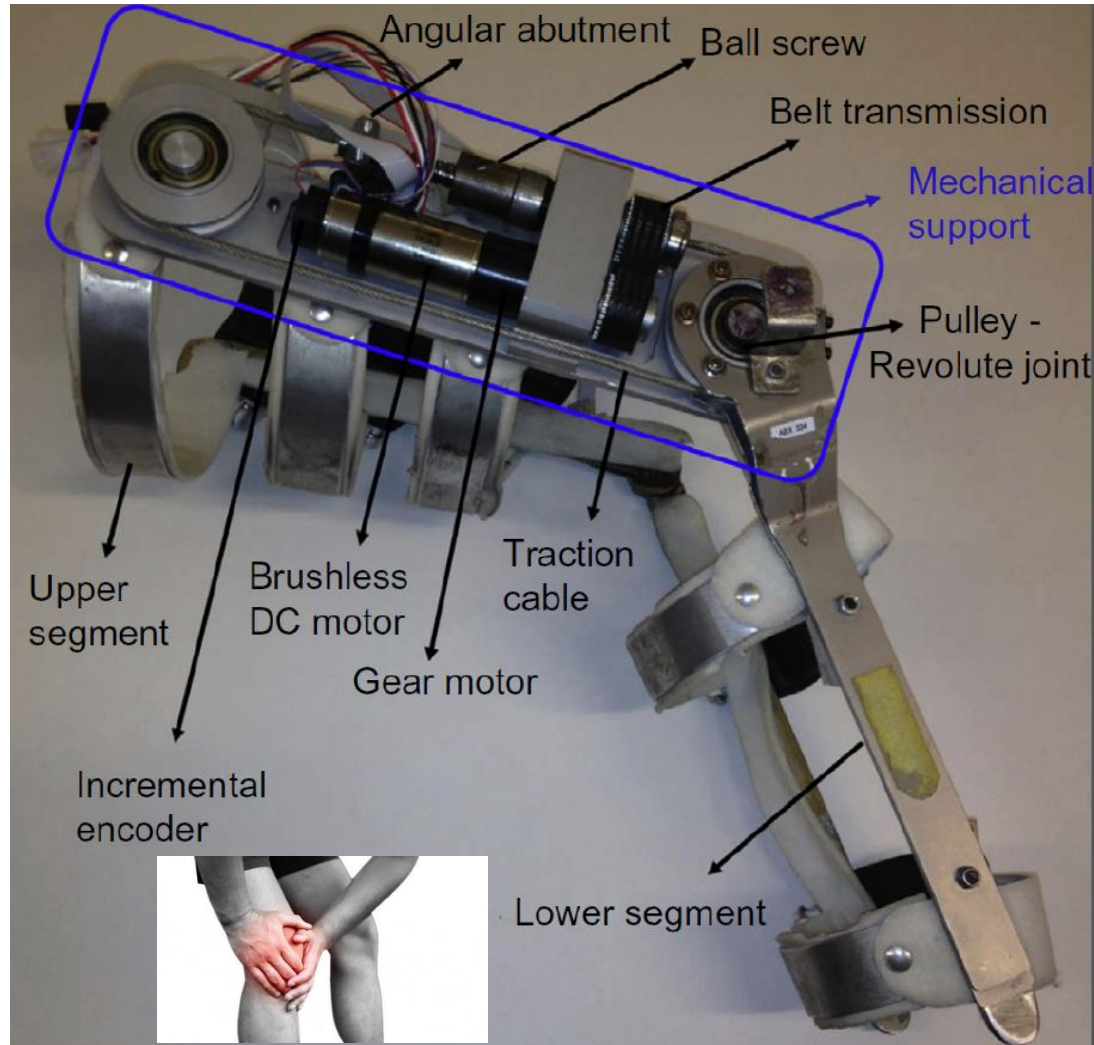
**Prototypes**

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## Overview of **EICOSI** exoskeleton (LISSI – UPEC)



For  
**knee Rehabilitation**

**EICOSI** : Exoskeleton Intelligently **CO**mmunicating and **S**ensitive to Intention

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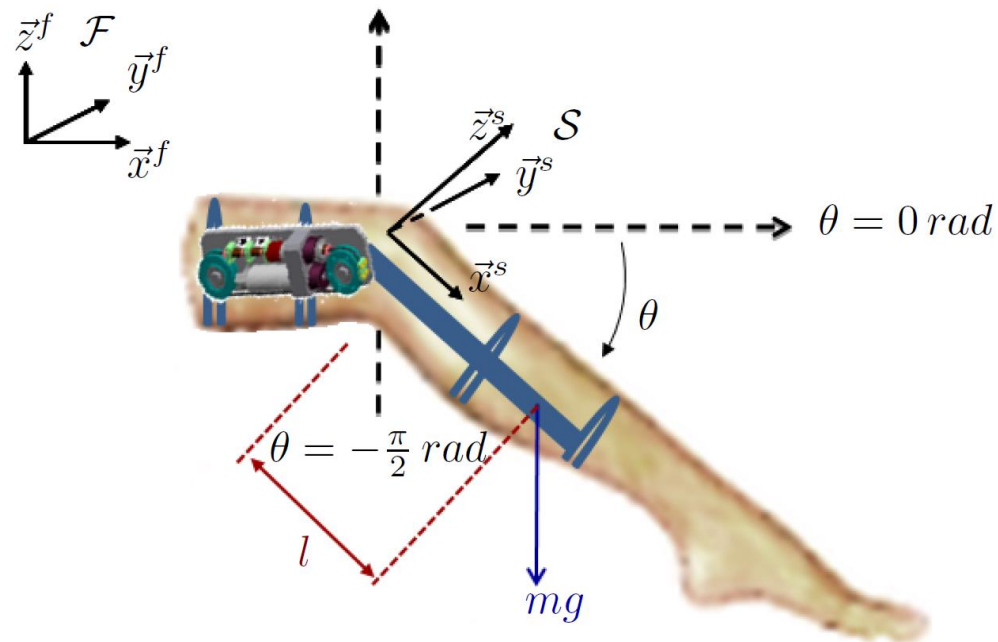
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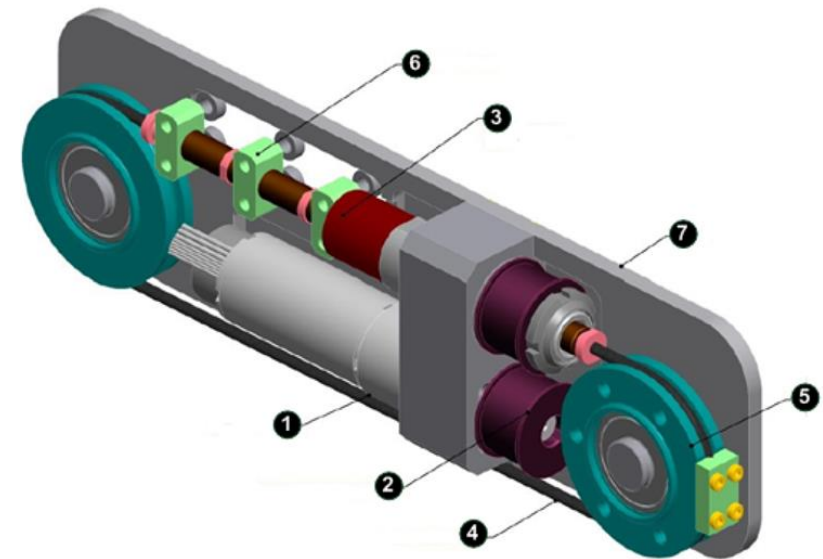
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Modelling & actuation of **EICOSI** exoskeleton

Its kinematics with human leg



Its actuation system



Its dynamic model

$$J\ddot{\theta} = -T_g \cos(\theta) - A \text{sign}(\dot{\theta}) - B\dot{\theta} + u + T_h$$



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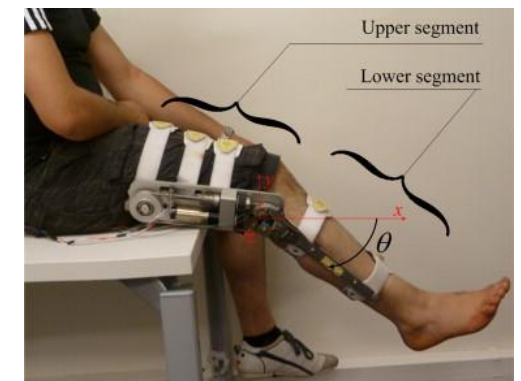
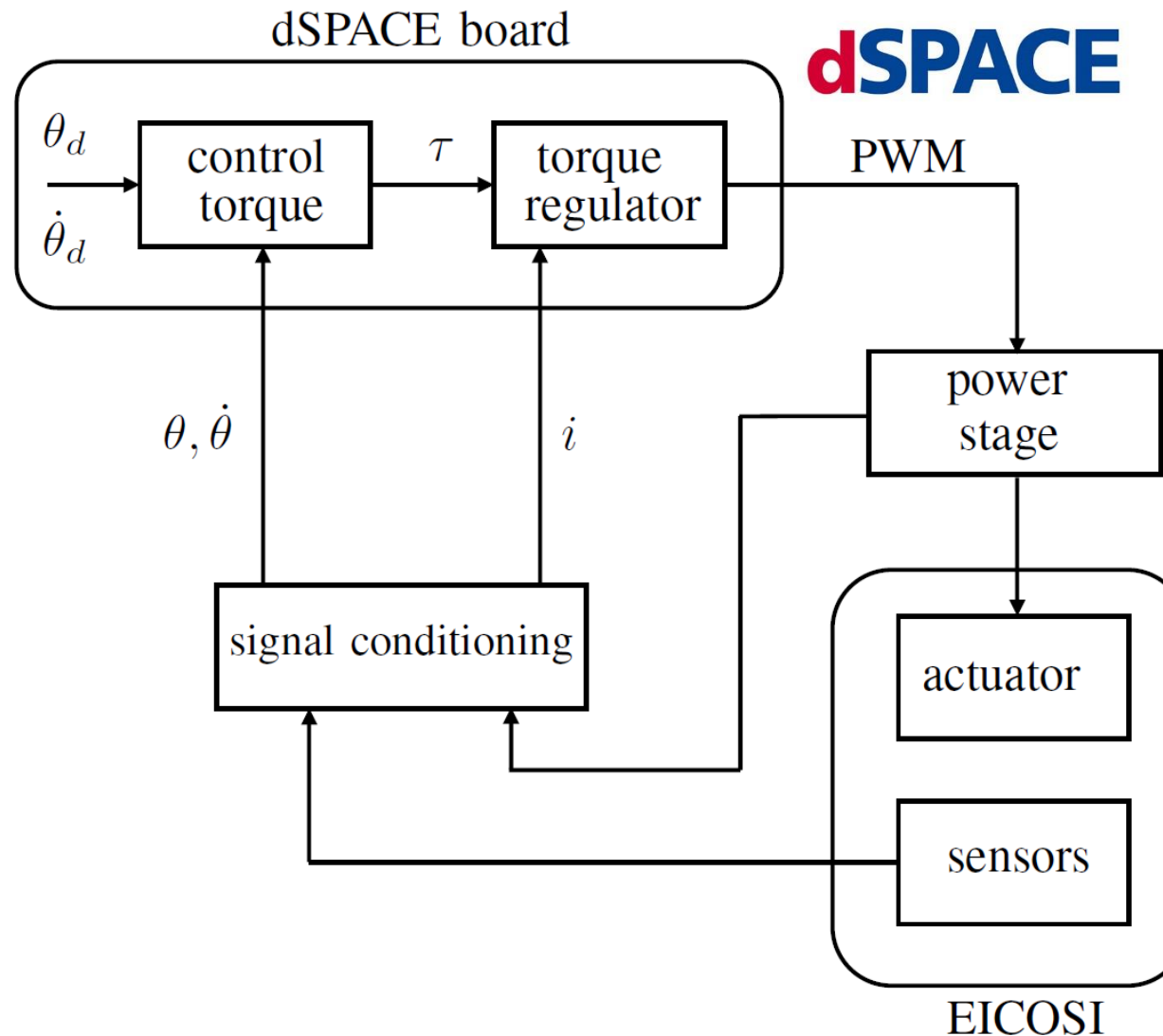
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## View of the hardware architecture of EICOSI exoskeleton



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Speaker : **A. CHEMORI**

## Typical applications of **EICOSI** exoskeleton



(a)



(b)



(c)



(d)



Site to stand task



Flexion-extension rehabilitation task



(a)



(b)



(c)



(d)

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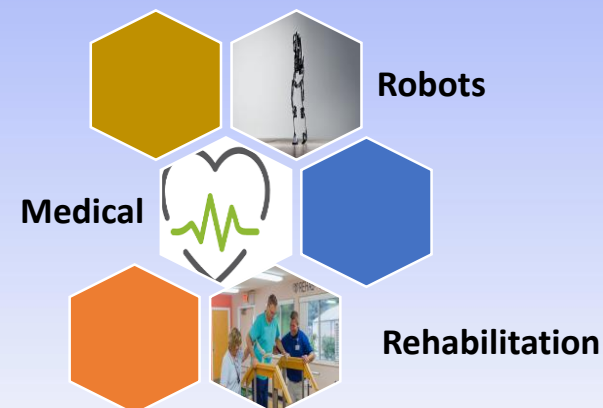
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# Proposed control solutions



# Proposed control solutions

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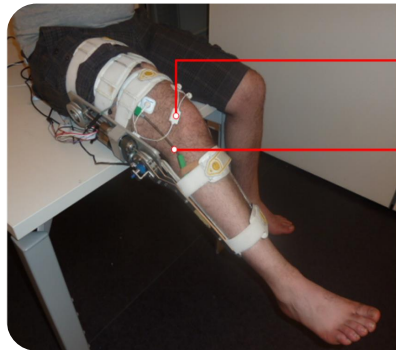
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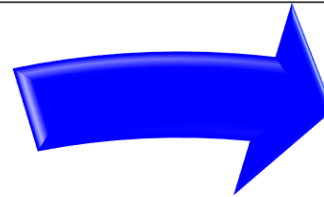
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$EMG$

$\theta_g$



## Three types of rehabilitations

1. Passive rehabilitation
2. Assistance as needed
3. Resistive rehabilitation

- ✓ PID controller
- ✓ Inverse dynamics control
- ✓ Sliding mode control
- ✓ **Model Predictive Control**
- ✓ **L1 adaptive control**
- ✓ Backstepping control
- ✓ RISE control
- ✓ NASF Control





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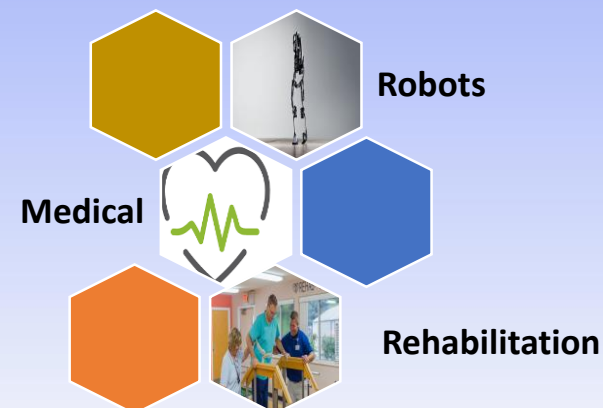
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# L1 Adaptive Control



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## Why L1 adaptive control ?

- ① Model **parameters** should be adequately **initialized**
- ② **Appropriate excitation** is needed for parameters convergence
- ③ **High** adaptation **gains** can **destabilize** the system



Proposed Solution

Decouple **Robustness** and **Adaptation**



Possibility of **zero**  
parameter  
**initialization**



**Large gains** lead to  
fast **adaptation** with  
**stability** guaranteed



Parameter **excitation**  
**not needed** for  
parameter convergence

**Solution :  $\mathcal{L}_1$  Adaptive controller** [Hovakimyan2010]

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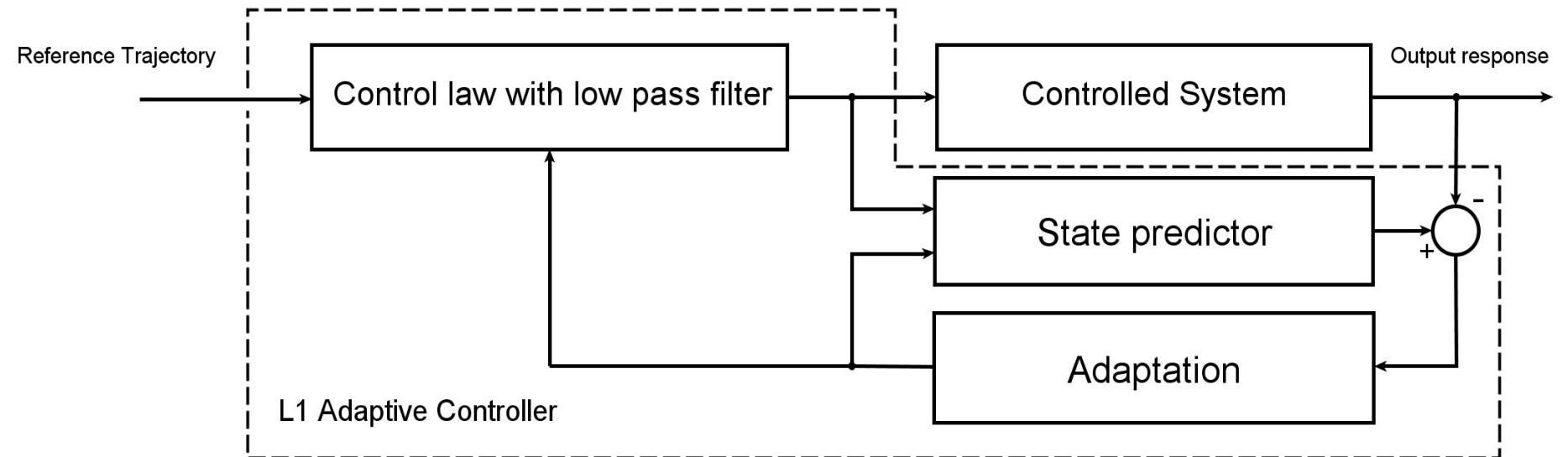
**Controllers**

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## Main features

- ✓ Recently developed controller [Hovakimyan 2010]
- ✓ Inspired from MRAC controller (+ low pass filter)
- ✓ Fast adaptation can be guaranteed
- ✓ Validated on various systems (mainly in aerospace)



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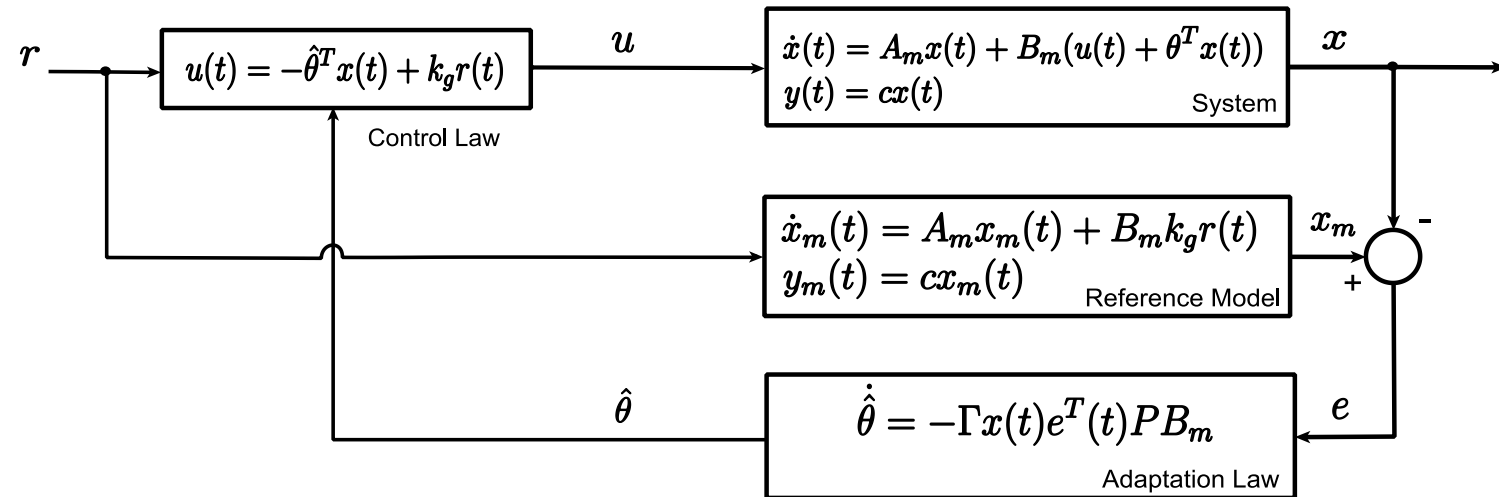
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✓ Inspired by direct **MRAC** (**M**odel **R**eference **A**daptive **C**ontrol)



$r$  : is a **piecewise-continuous bounded** reference signal

$\theta$  : is a vector of **unknown** constant parameters

$\hat{\theta}$  : is the **estimate** of  $\theta$

$$k_g = \frac{-1}{c A_m^{-1} B_m}$$

$$P = P^T$$

$$A_m^T P + P A_m = -Q$$

$$Q = Q^T > 0$$



# L1 Adaptive control

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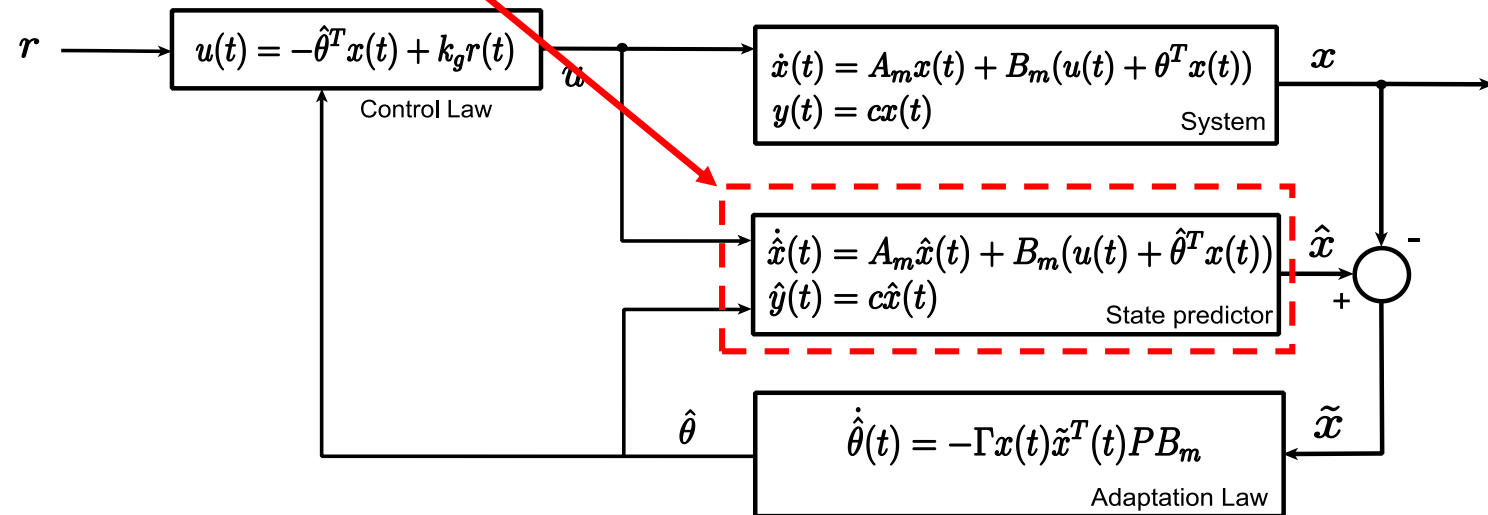
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- ✓ Inspired by direct **MRAC** (Model Reference Adaptive Control)
- ✓ With a **State predictor** instead of the **reference model**



- ✓ The tracking error is replaced by the prediction error

# L1 Adaptive control

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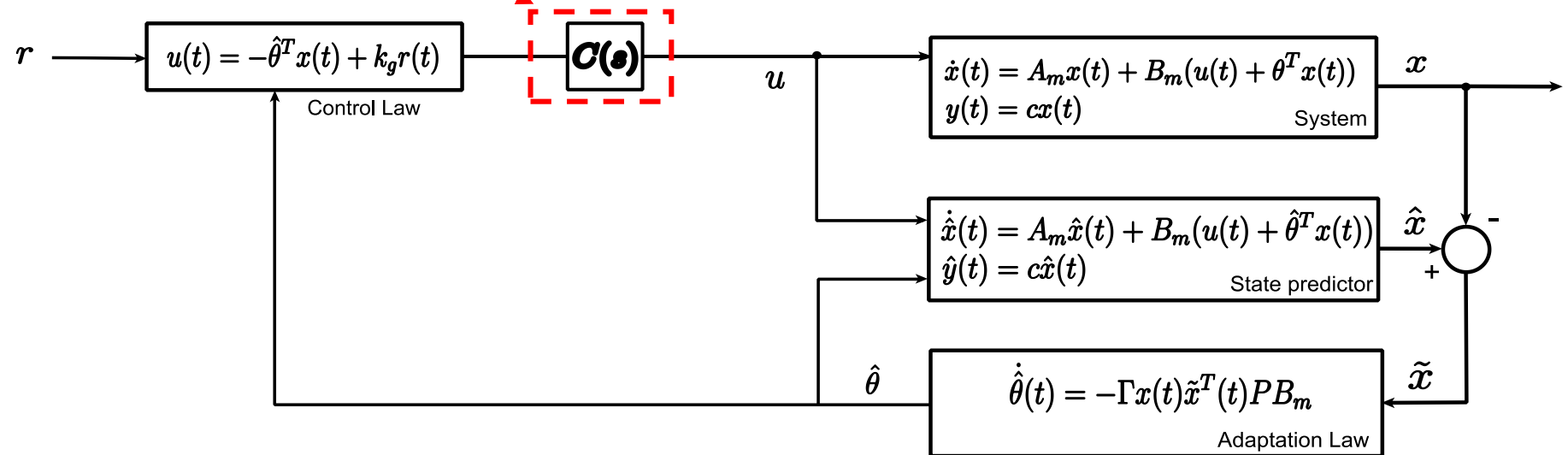
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- ✓ Inspired by direct **MRAC** (**M**odel **R**eference **A**daptive **C**ontrol)
- ✓ With a **State predictor** instead of the **reference model**
- ✓ With **low pass filter**



$C(s)$  : is a **stable** and **strictly proper** transfer function

$C(s) = 1 \rightarrow$  Direct MRAC

# L1 Adaptive control

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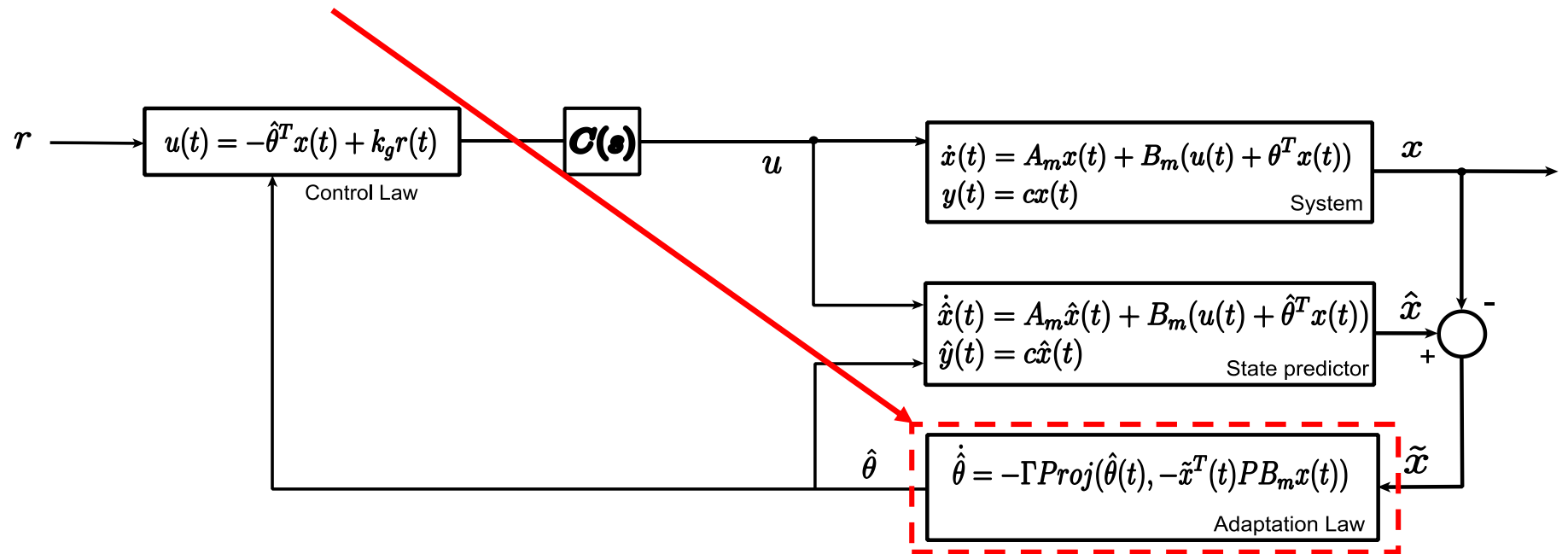
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- ✓ Inspired by direct **MRAC** (**M**odel **R**eference **A**ddaptive **C**ontrol)
- ✓ With a **State predictor** instead of the **reference model**
- ✓ With a **low pass filter**
- ✓ With a **projection operator** to bound the estimated parameters





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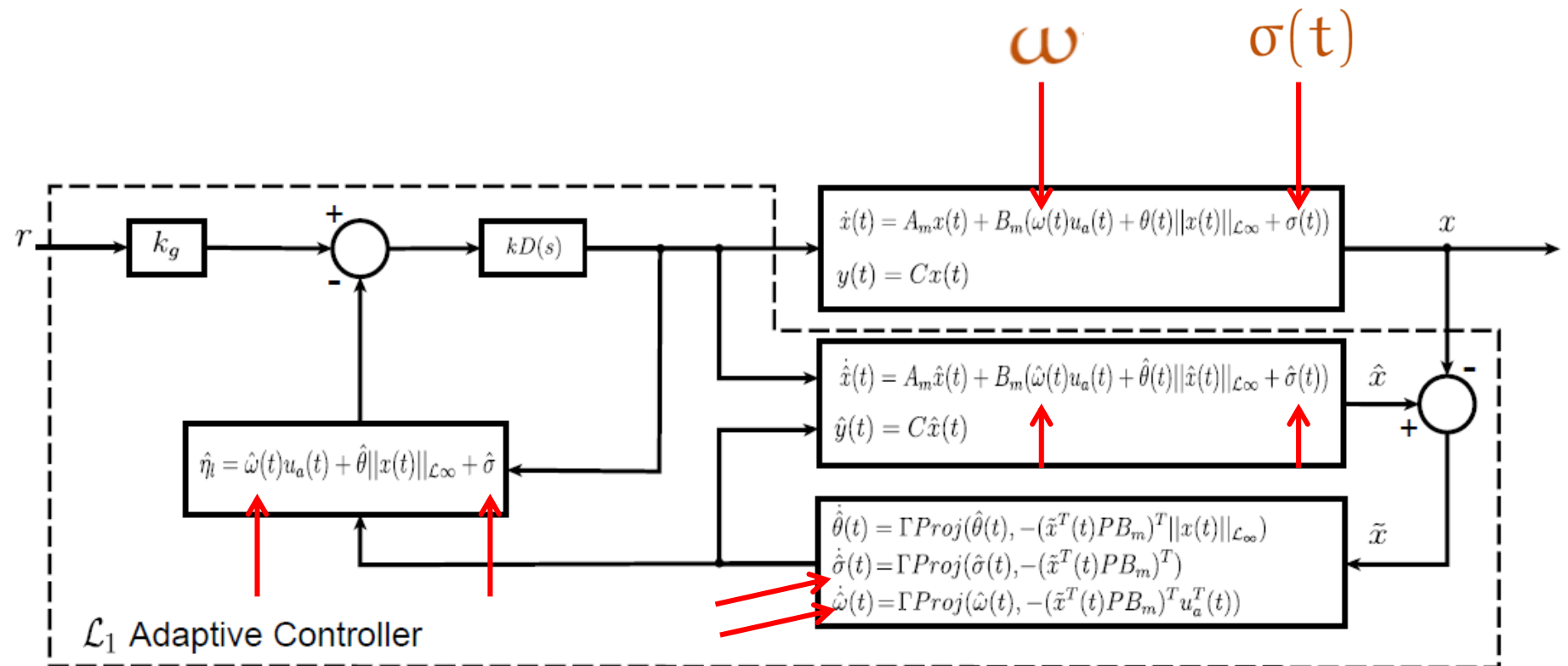
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## Case of Multi-Input Multi-Output form with 2 additional parameters to estimates



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## Motivation : Time lag limitation

Consider the following system [Hovakimyan 2010]

$$\dot{x}(t) = Ax(t) + B(u(t) + \theta(t)^T x(t)) \quad , \quad x(0) = x_0$$

$$y(t) = Cx(t)$$

$$A = \begin{bmatrix} 0 & 1 \\ -1 & -1.4 \end{bmatrix} \quad ; \quad B = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \quad ; \quad C = [1 \quad 0] \quad ; \quad \theta = \begin{bmatrix} 4 \\ -4.5 \end{bmatrix}$$

The proposed design parameters are the following:

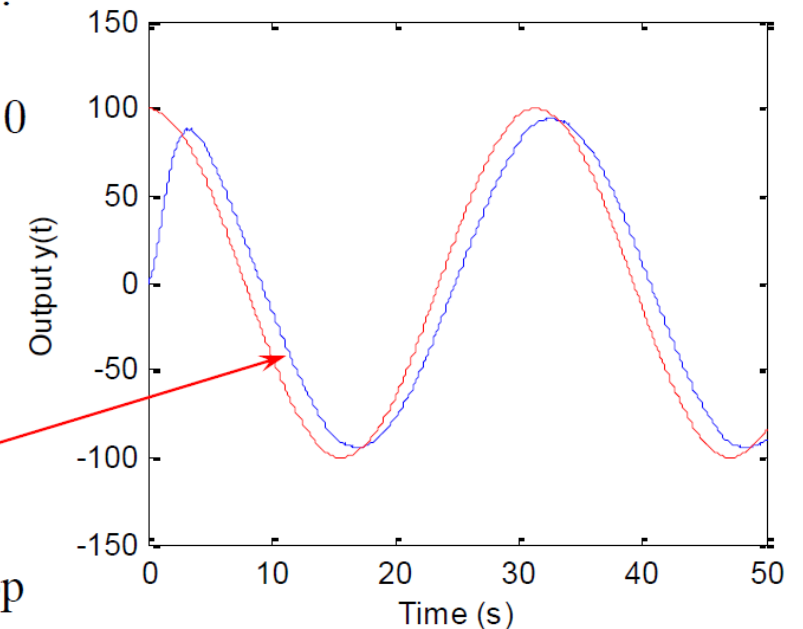
$$C(s) = \frac{\omega_k D(s)}{1 + \omega_k D(s)} = \frac{160}{s + 160} \quad , \quad \Gamma = 10000 \quad , \quad k_m = 0$$

For a bounded reference trajectory to be tracked :

$$r(t) = 100 \cos(0.2t)$$

A time lag in the tracking is noticed

Due to the presence of the filter in the control loop



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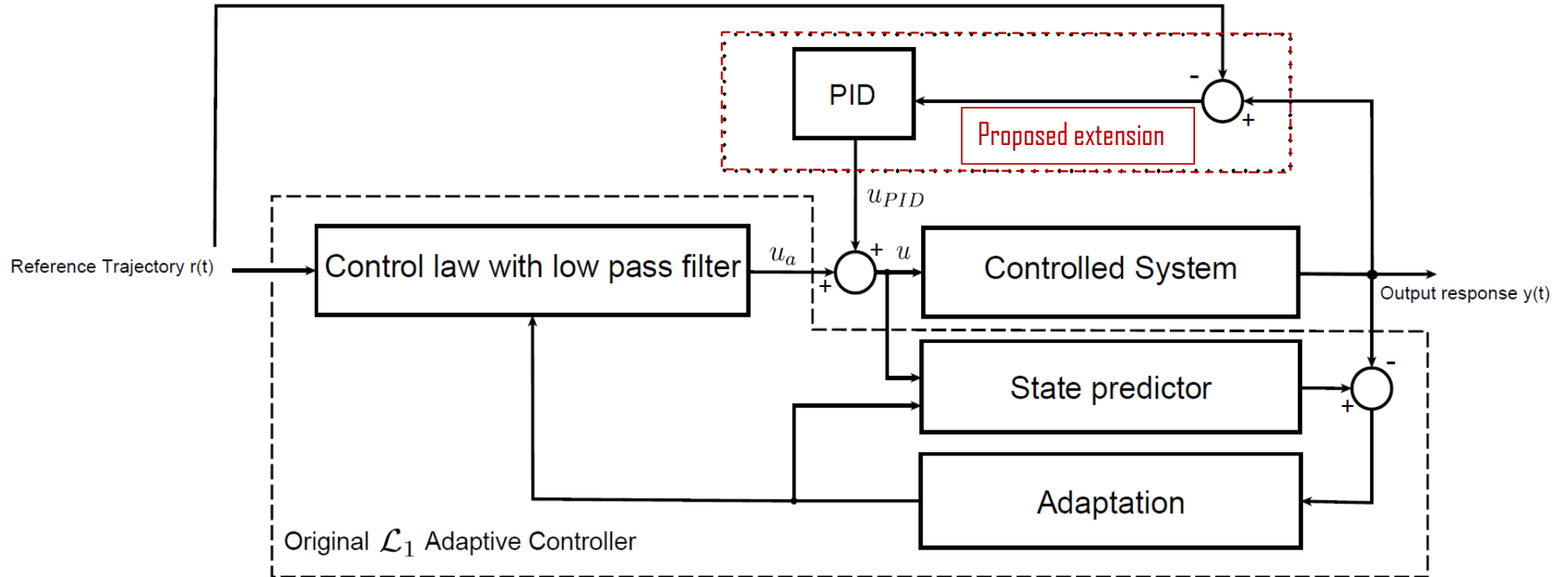
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## Proposed solution : Basic idea



The new control law in this case :  $u = u_a + u_m + u_{PID}$

The adaptive term  
The state-feedback term  
The proposed extension term



## First validation : Back to the example

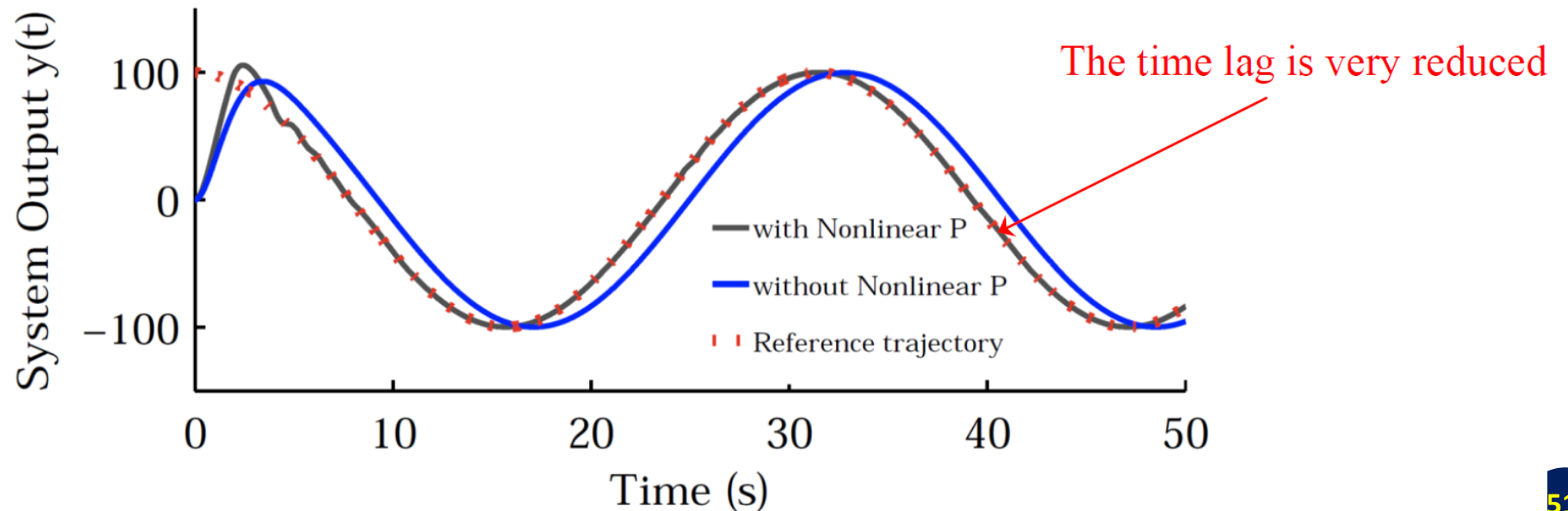
The proposed design parameters are the same:

$$C(s) = \frac{160}{s+160} \quad , \quad \Gamma = 10000 \quad , \quad k_m = 0$$

The same reference trajectory to be tracked :

$$r = 100 \cos(0.2t)$$

The obtained tracking for both controllers :



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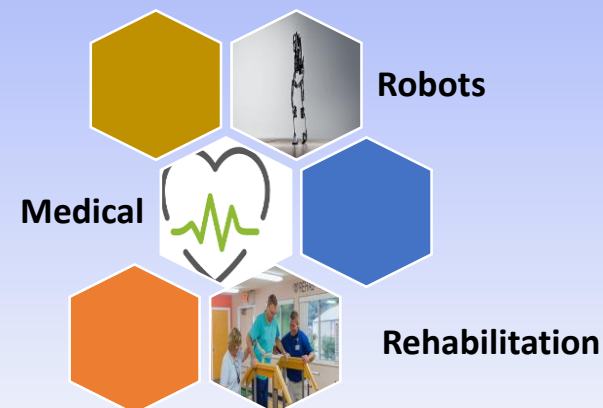
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# Experimental results

## L1 Adaptive



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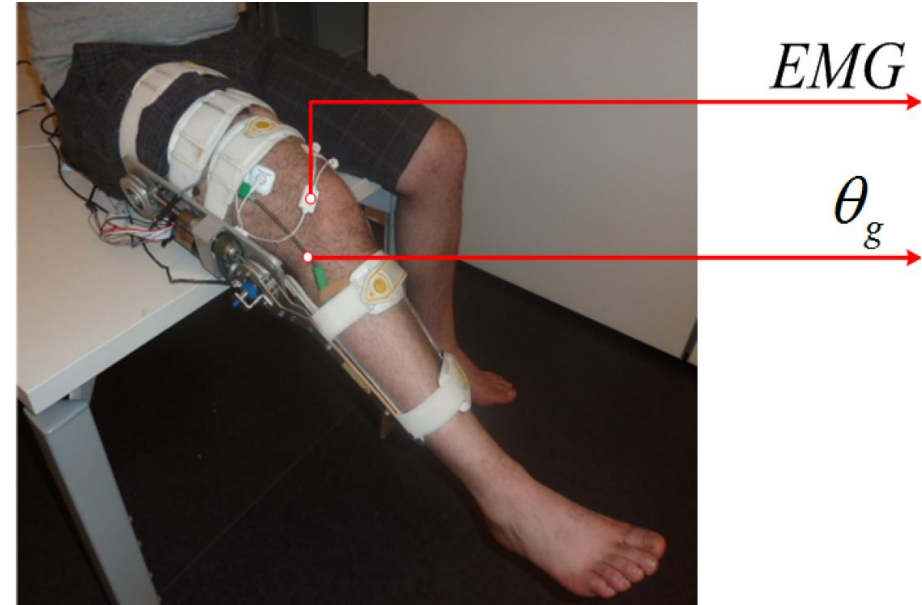
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## Some experimental issues

- ✓ Performed on a healthy male subject,
- ✓ 23 years old,
- ✓ Weighing 65 Kg, and
- ✓ Measuring 178 cm



### EMG electrodes are used :

- ✓ At the **rectus femoris** (RF) acting as a quadriceps muscle and the **biceps femoris** long head (BF) acting as hamstring muscle
- ✓ The EMG measurements are presented only to show the muscles activity and are not used in the control law

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## Some experimental issues

- ✓ All the estimated parameters have been initialized to zero
- ✓ The parameters of the state feedback are taken as:  $k_{m1} = 1$  and  $k_{m2} = 1,4$
- ✓ **Classical** and **augmented L1** adaptive control laws are compared

**Three case studies have been performed :**

- ✓ **Scenario 1** : Passive rehabilitation
- ✓ **Scenario 2** : Assistance as needed
- ✓ **Scenario 3** : Resistive rehabilitation



# Real-time experimental results

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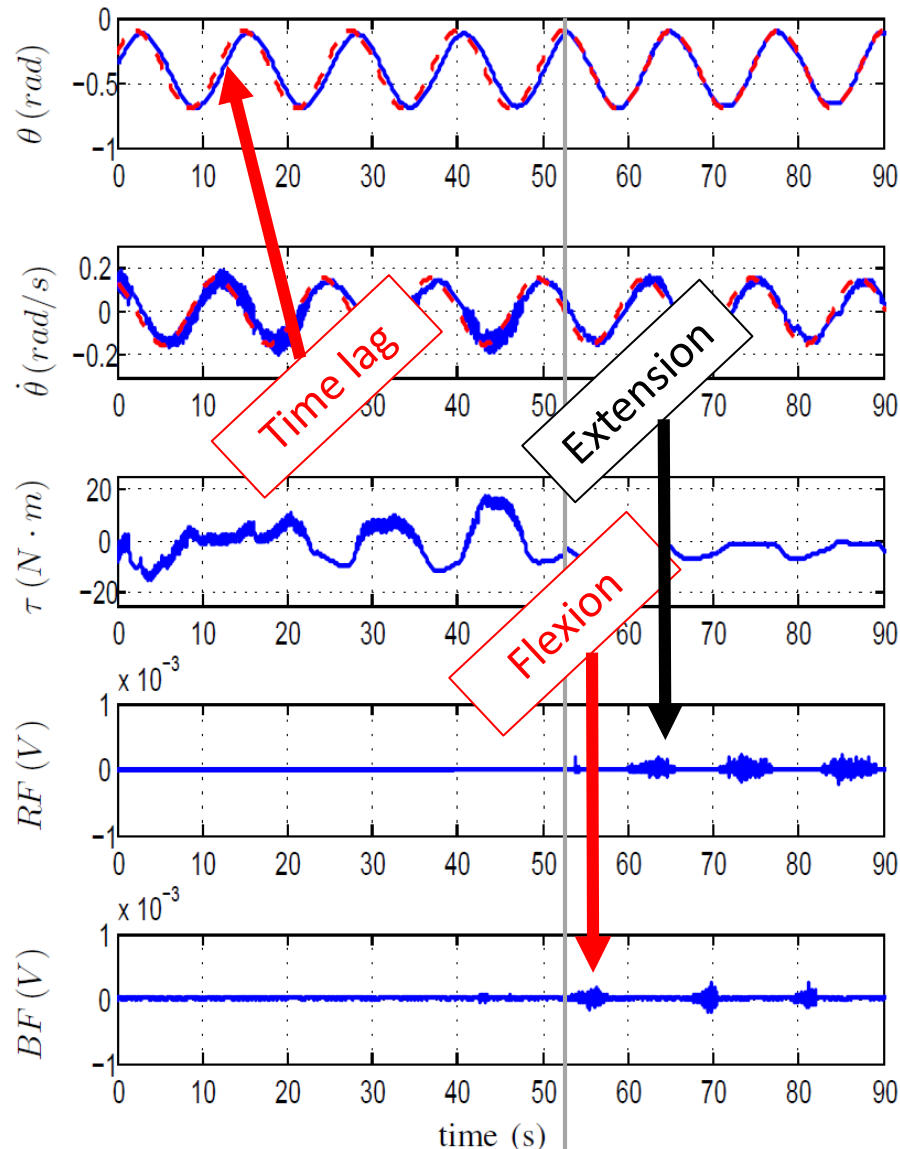
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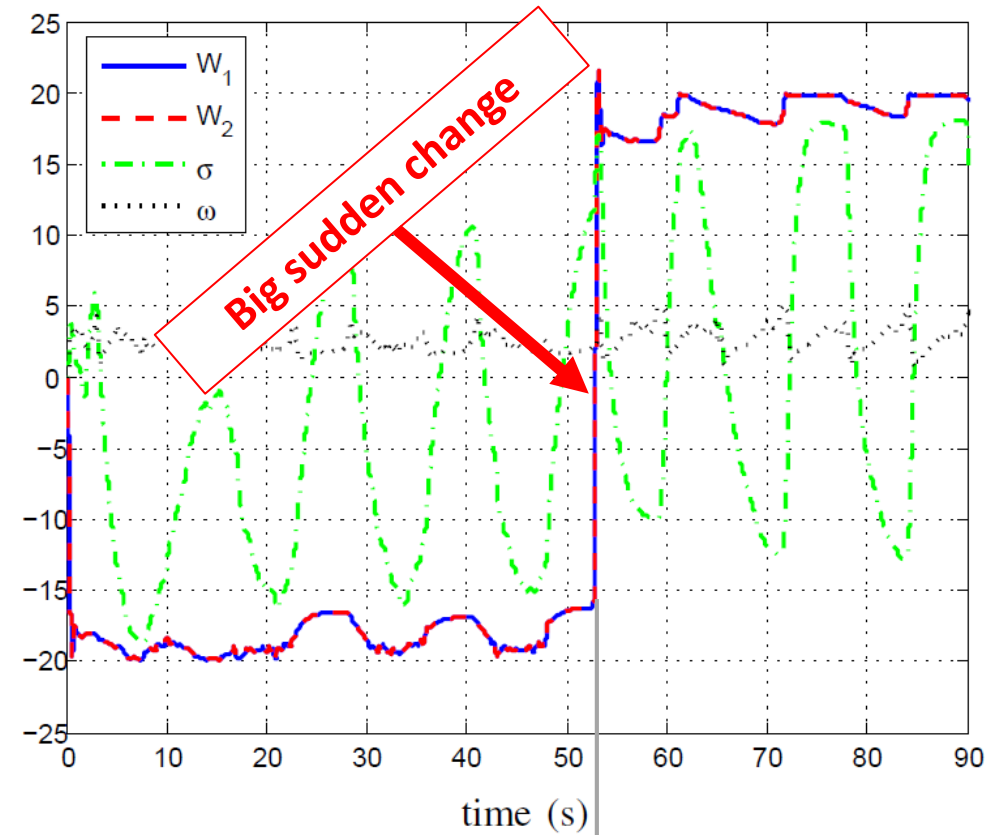
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## Scenario 2 : Assistance as needed

### L1 adaptive control



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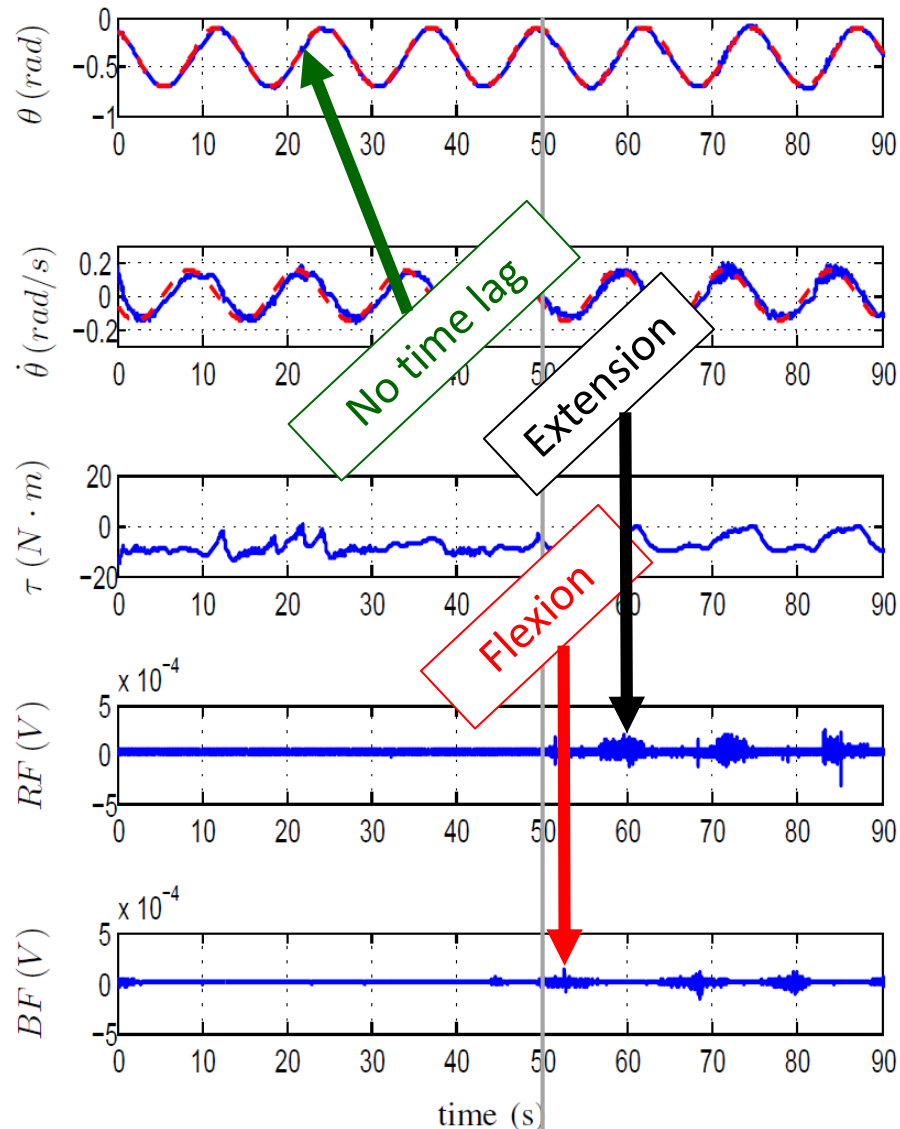
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Speaker : A. CHEMORI

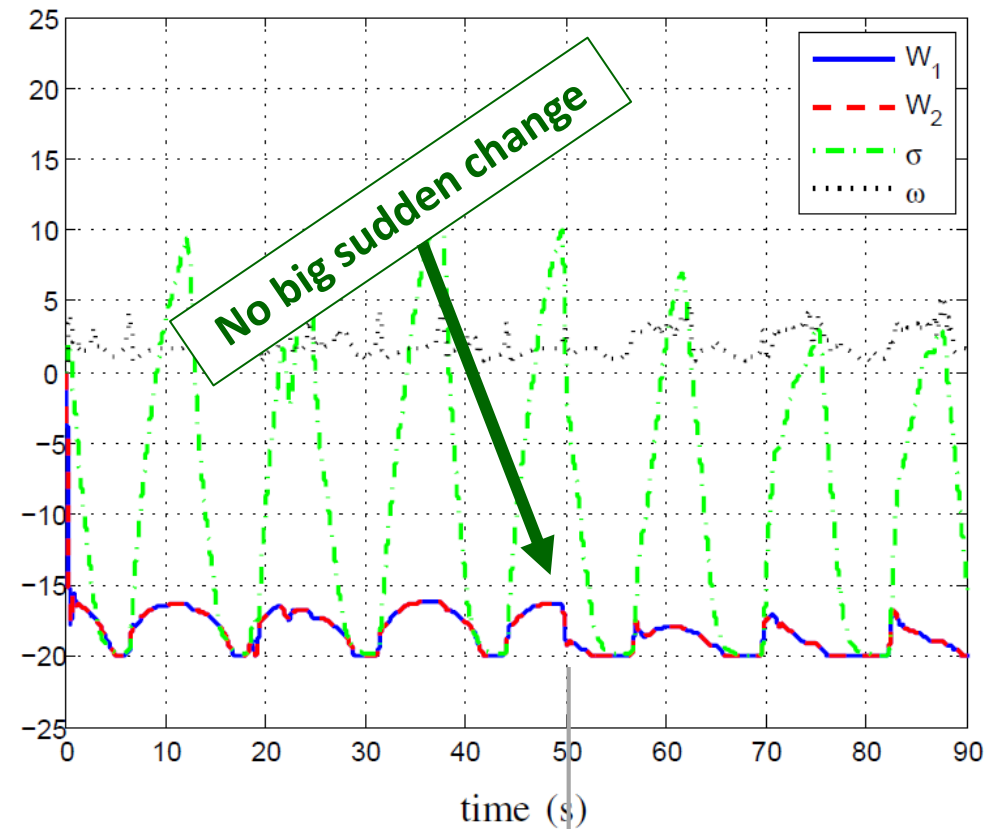


Passive wearer

Active wearer

## Scenario 2 : Assistance as needed

### Augmented L1 adaptive control



Passive wearer

Active wearer

# Real-time experimental results

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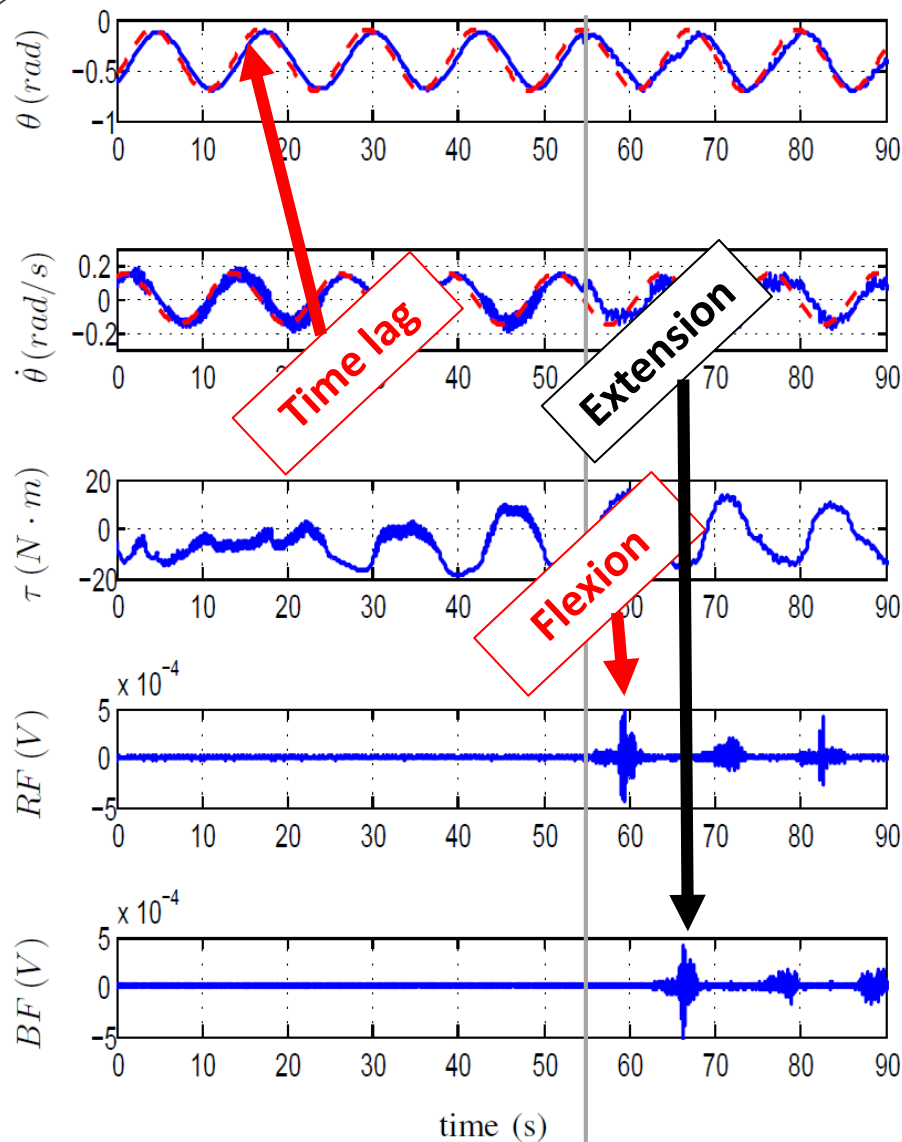
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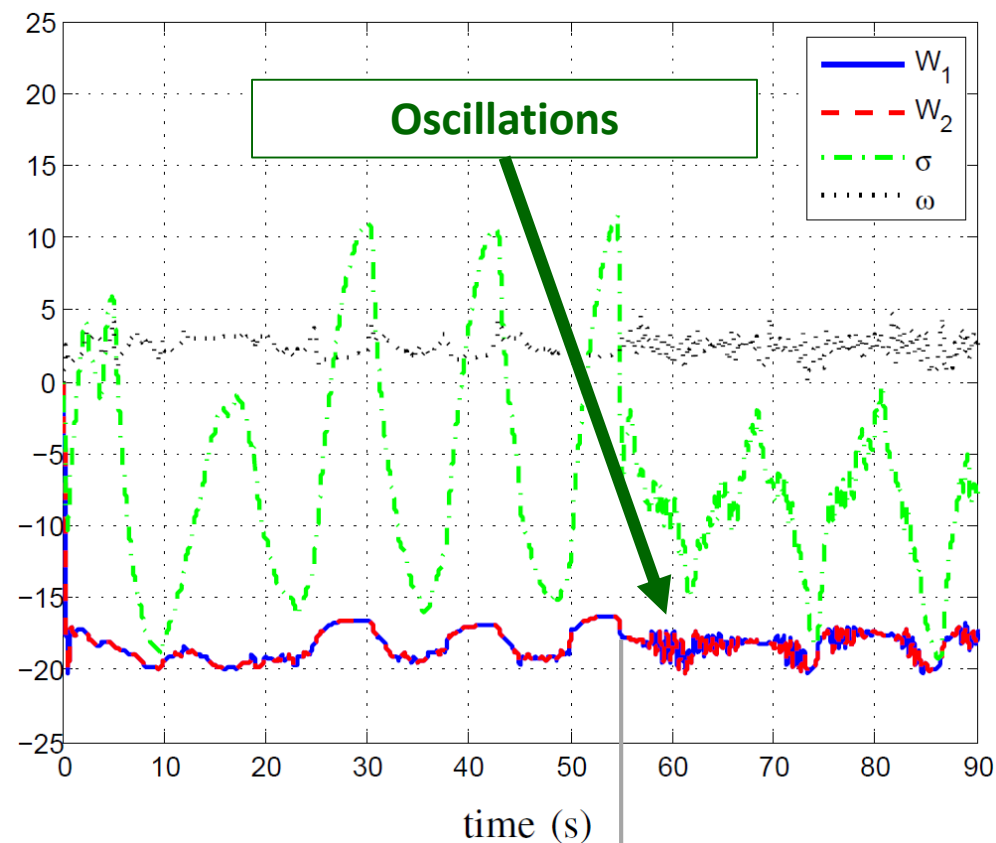


Passive wearer

Active wearer

## Scenario 3 : Resistive rehabilitation

### L1 adaptive control



Passive wearer

Active wearer

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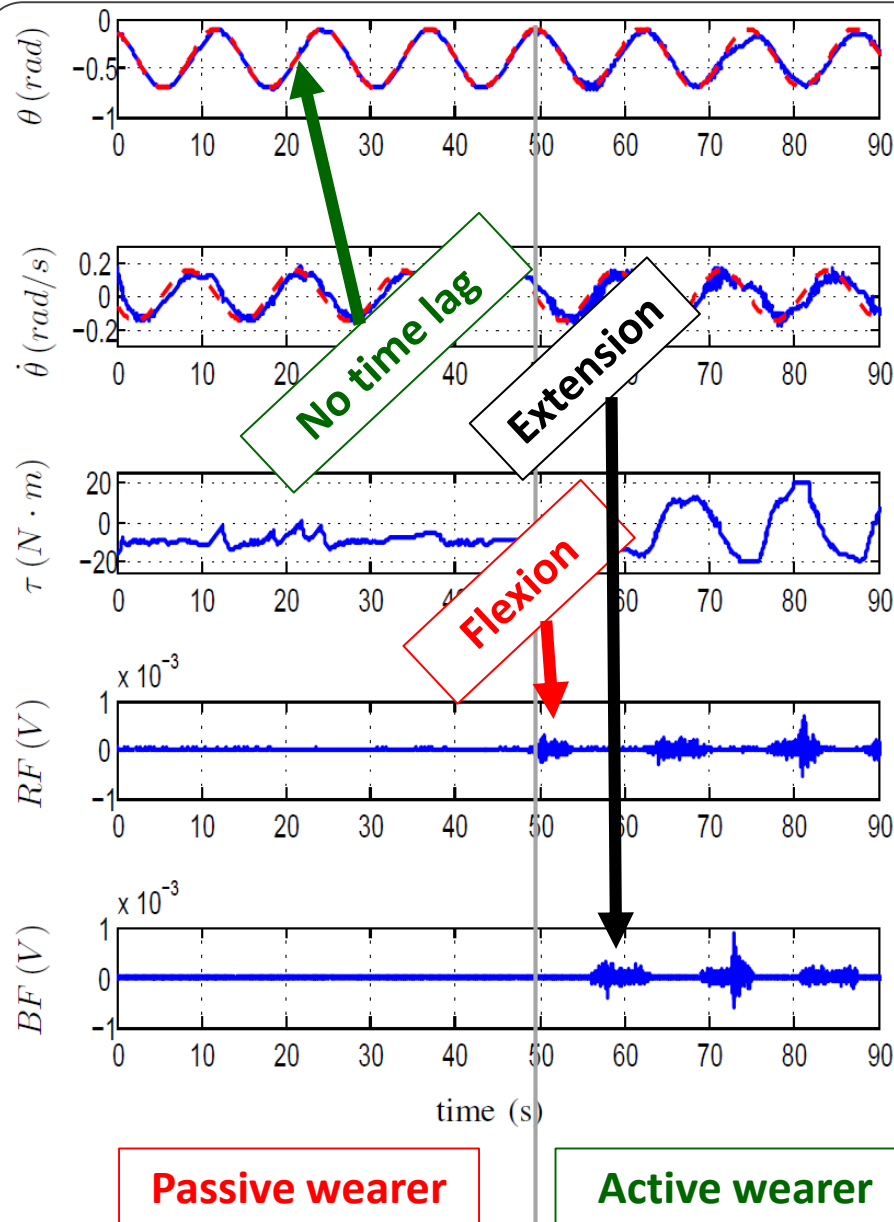
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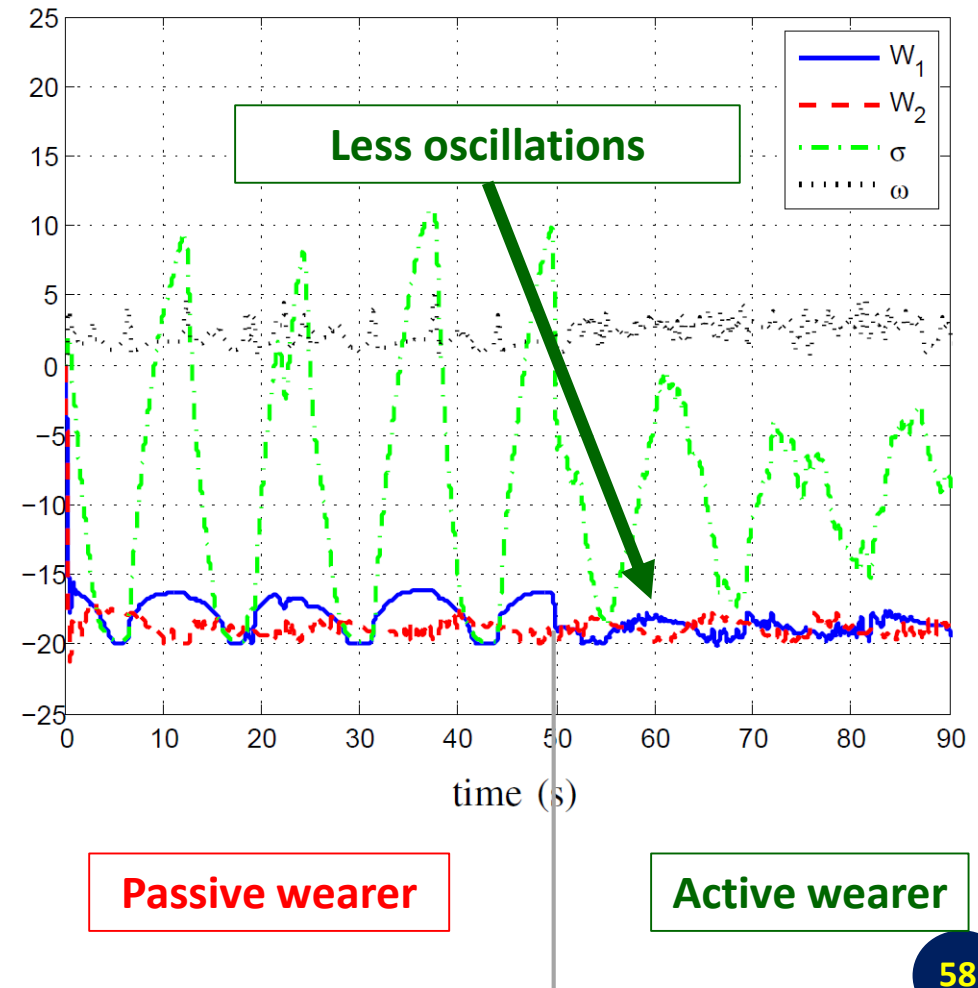
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## Scenario 3 : Resistive rehabilitation

### Augmented L1 adaptive control





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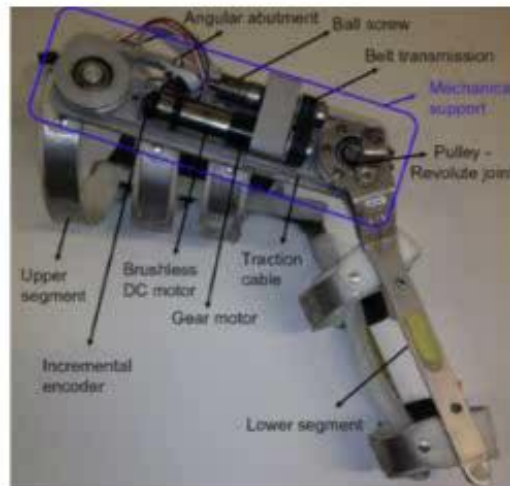
Speaker : **A. CHEMORI**



## Augmented L1 Adaptive Control of an Actuated Knee Joint Exoskeleton

### - Real-Time Experimental results -

H. Rifai<sup>1</sup>, M.S. Ben Abdesslem<sup>1</sup>, A. Chemori<sup>2</sup>, S. Mohammed<sup>1</sup> and Y. Amirat<sup>1</sup>



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[Rifai et al 2016] H. Rifai, M-S. Ben Abdesslem, A. Chemori, S. Mohammed and Y. Amirat, "Augmented L1 Adaptive Control of an Actuated Knee Joint Exoskeleton: From Design to Real-Time Experiments", IEEE ICRA'16, Stockholm, Sweden, 2016.

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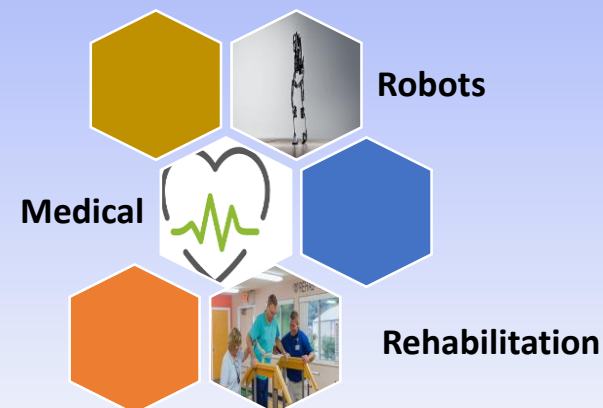
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# MPC – Based Control



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This article has been accepted for inclusion in a future issue of this journal. Content is final as presented, with the exception of pagination.

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## An Assistive Explicit Model Predictive Control Framework for a Knee Rehabilitation Exoskeleton

Ines Jammeli, Ahmed Chemori, Senior Member, IEEE, Huiyeok Moon, Salwa Elloumi, and Samer Mohammed, Senior Member, IEEE

**Abstract**—This article focuses on the control of an actuated knee joint orthosis. The proposed solution is a novel model predictive control framework dedicated to assistive and rehabilitation purposes. This framework includes 1) an exact input-to-state feedback linearization, 2) a model predictive controller (MPC or EMPC), considering input/output constraints, 3) a least-squares dynamic parameters identification, 4) a nonlinear disturbance observer for the estimation of the wearer's torque, 5) a Lyapunov-based stability analysis of the resulting closed-loop system, and 6) a reference trajectory generator. The proposed framework has been validated via real-time experiments performed on three healthy subjects wearing the knee joint orthosis. Various experimental scenarios have been considered, including assistive and resistive rehabilitation tasks in a sitting position and walking with normal/abnormal gait patterns. The obtained results indicate the efficiency of the proposed predictive controllers with respect to a conventional proportional-integral-derivative (PID) controller in terms of tracking performance, required torque, and wearer comfort.

**Index Terms**—Assistive robotics, knee joint powered orthosis, model predictive control (MPC), rehabilitation.

### I. INTRODUCTION

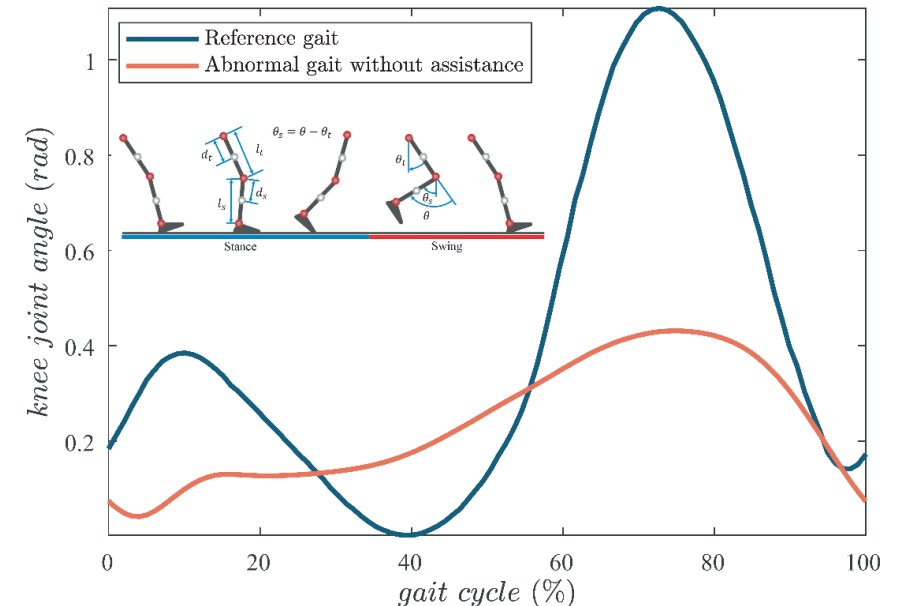
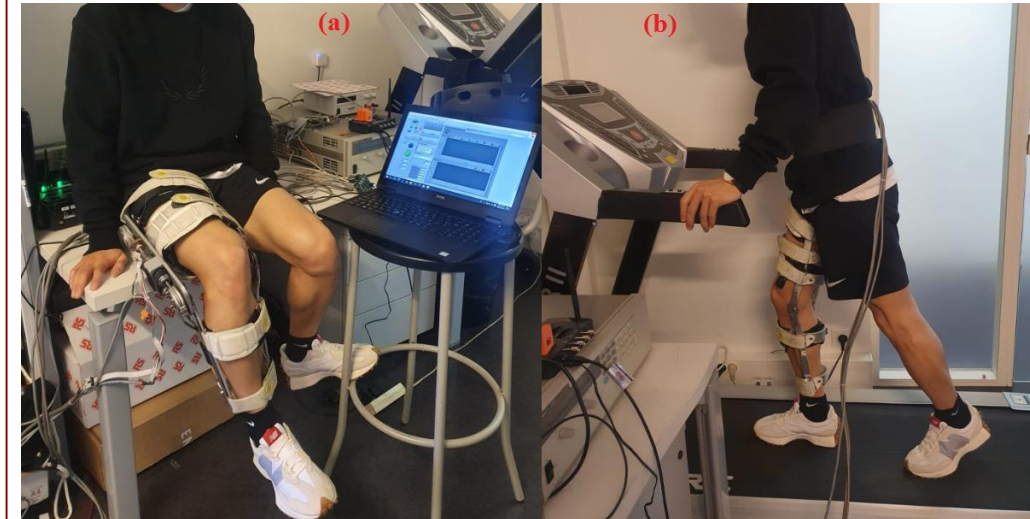
WITH recent medical advances, life expectancy increases steadily. According to the World Health Organization, the world population aged 60 years and older is expected to reach a total of 2 billion by 2050; however, it was approximately 900 million in 2015. This population is exposed to health risks

caused by weakened muscle strength, which hinders their ability to walk as frequently as normal and adversely affects their walking stability, thereby making them dependent on others. Consequently, the aging of the population and the physical deterioration of the elderly have become a global socioeconomic problem [1]. This issue calls for considerable attention on how to assist this population, as well as people with lower and/or upper-limb pathologies in their daily life, especially regarding mobility and autonomy [2].

One of the best remedies for reduced mobility is rehabilitation. Conventional intensive therapies are usually adopted in clinical centers to help people recover their voluntary movements. However, the problem with these therapies is that they are only effective when they are intensive [3]. Furthermore, repetition is a key element in this case, which allows the brain to reprogram the motion sequence. Therefore, this process is time and capital intensive, and requires the strength of both the patient and therapist. However, intensive long-term rehabilitation therapy is not always an option owing to its expensive cost, and the insufficiency of qualified staff.

To reduce the burden on care services, several initiatives have been set up to promote assistive technologies, such as the promising technologies based on wearable robots. These devices are mechatronic systems, equipped with sensors and actuators, and embodied by the human upper and/or lower-limbs, which provide the following functions: 1) augmenting physical human capabilities at upper/lower-limbs, 2) assisting people with reduced mobility for achieving daily living activities, and 3) automating the rehabilitation of human joints and muscles to recover and improve the control of the wearer's limbs [4]. This considerable focus on wearable robots can be explained by their ability to reproduce repetitive tasks that require strength and robustness. They can autonomously perform these tasks faster than therapists, with a better level of accuracy, without getting tired, and without requiring a third party. Hence, they may promote a reduction in patient fatigue. They enable long training sessions with optimal consistency, as well as measurements for the user to track the desired gait patterns, which may help to accelerate the rehabilitation process [5].

Sitting and standing up movements are essential for most human activities. Given their importance, several wearable robots have been developed to help weakened people perform these movements. Shepherd *et al.* [6] designed a knee exoskeleton



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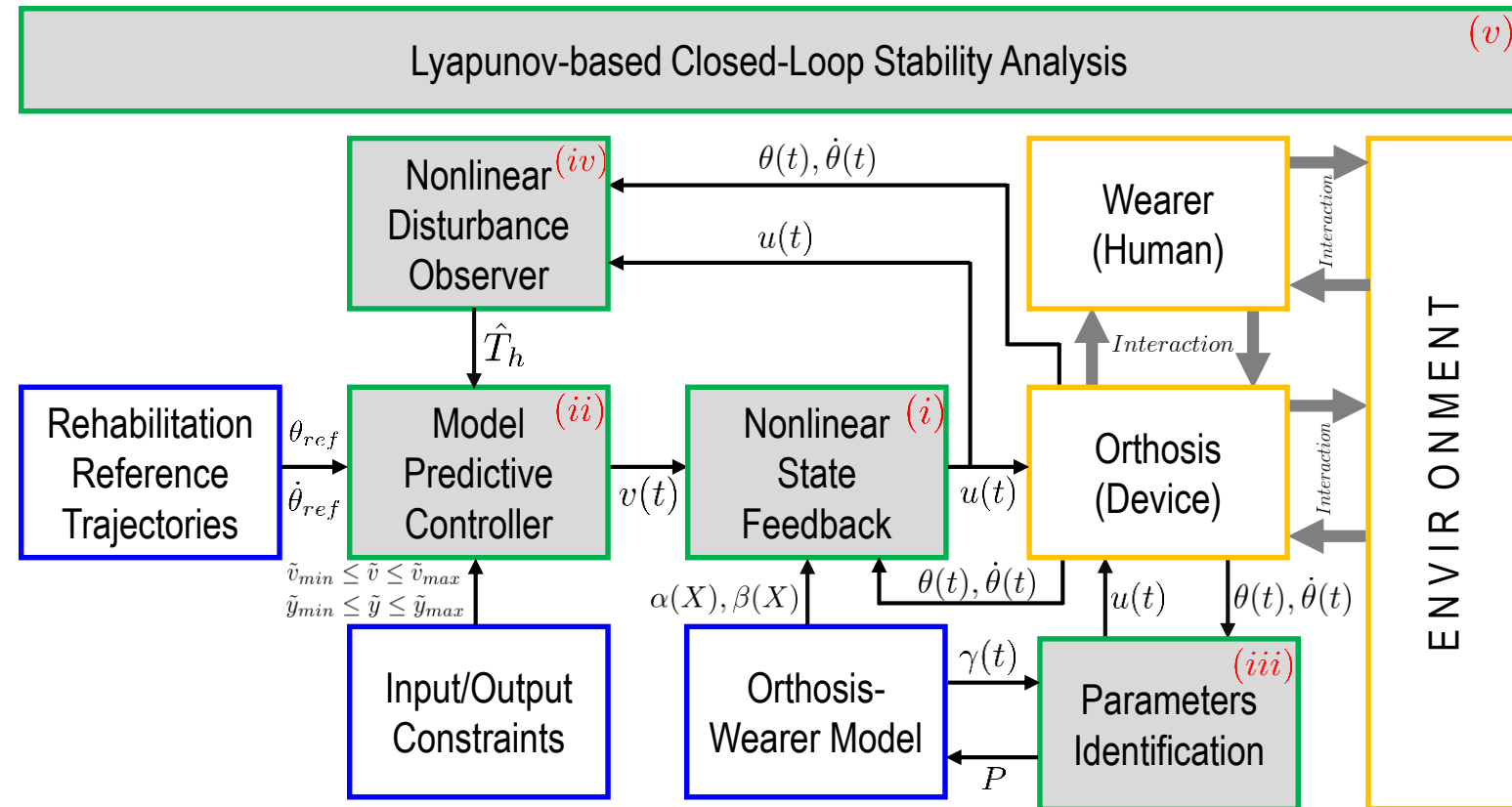
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## Proposed MPC-Based control framework





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## Identification of dynamic parameters

(iii)  
Parameters  
Identification

- ✓ The subject wear the exoskeleton, stay passive in a sitting position
- ✓ The human-orthosis is considered to be a single system
- ✓ Its inverse dynamic model can be represented as:

$$\tau_e = J\ddot{\theta} - T_g \cos(\theta) + A \text{Sign}(\dot{\theta}) + B\dot{\theta}$$

- ✓ Which can be rewritten in an affine in the parameters as follows:

$$\tau_e(t) = \begin{bmatrix} -\cos(\theta(t)) & \text{Sign}(\dot{\theta}(t)) & \dot{\theta}(t) & \ddot{\theta}(t) \end{bmatrix} \begin{pmatrix} T_g \\ A \\ B \\ J \end{pmatrix}$$

$$= \gamma^T(t)P$$

- ✓ A least square method is used

Parameter	Symbol	S1	S2	S3
Static friction coefficient ( $N.m$ )	$A$	2.0082	1.2067	0.7613
Viscous friction coefficient $N.m.s.rad^{-1}$	$B$	1.713	3.238	2.4539
Inertia $Kg.m^2$	$J$	0.4325	0.2594	0.2525
Gravity torque ( $N.m$ )	$T_g$	9.4199	10.4741	3.4379

## Input-to-state feedback linearization

Nonlinear <sup>(i)</sup>  
State  
Feedback

- ✓ Let us consider the nonlinear state feedback:

$$\tau_e = \alpha(X) + \beta(X)v$$

- ✓ For the sitting position, we set:

$$\begin{cases} \alpha(X) = -T_g \cos(\theta) + ASign(\dot{\theta}) + B(\dot{\theta}) - \tau_h \\ \beta(X) = J \\ X = [x_1 \ x_2]^T = [\theta \ \dot{\theta}]^T \end{cases}$$

- ✓ Then the resulting nonlinear state feedback writes:

$$\tau_e(t) = -T_g \cos(\theta) + ASign(\dot{\theta}) + B(\dot{\theta}) - \tau_h + Jv.$$

- ✓ For the standing position, we set:

$$\begin{cases} \alpha(X) = T_g \sin(\theta - \theta_t) + ASign(\dot{\theta}) + B(\dot{\theta}) - \tau_h + \tau_l \\ \beta(X) = J \\ X = [x_1 \ x_2]^T = [\theta \ \dot{\theta}]^T \end{cases}$$

- ✓ Then the resulting nonlinear state feedback writes:

$$\tau_e(t) = T_g \sin(\theta - \theta_t) + ASign(\dot{\theta}) + B(\dot{\theta}) - \tau_h + \tau_l + Jv \quad (1)$$

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## Input-to-state feedback linearization

Nonlinear <sup>(i)</sup>  
State  
Feedback

- ✓ The nonlinear state feedback, replaced in the orthosis dynamics leads to:

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = v \\ y = x_1 \end{cases}$$

- ✓ The discretization of the resulting linear dynamics using Euler's method leads to :

$$\begin{cases} \tilde{X}(k+1) = A\tilde{X}(k) + B\tilde{v}(k) \\ \tilde{y}(k) = C\tilde{x}(k) \end{cases}$$

- ✓ With:

$$A = \begin{pmatrix} 1 & T_s \\ 0 & 1 \end{pmatrix}, \quad B = \begin{pmatrix} 0 \\ T_s \end{pmatrix}, \quad \text{and} \quad C = (1 \quad 0)$$

- ✓ The proposed MPC controller is designed based on this dynamics.

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## Proposed MPC controller

Model (ii)  
Predictive  
Controller

- ✓ The associated optimization problem can be expressed as:

$$V(k) = \min \left( \frac{1}{2} \tilde{v}_{\rightarrow k}^T H \tilde{v}_{\rightarrow k} + \tilde{X}(k)^T F \tilde{v}_{\rightarrow k} \right) + \frac{1}{2} \tilde{X}(k)^T Y \tilde{X}(k)$$

$$\left\{ \begin{array}{l} \text{s.t } \theta_{\min} \leq \theta(k+i) \leq \theta_{\max} \quad \text{for } i = 1..N_c \\ \dot{\theta}_{\min} \leq \dot{\theta}(k+i) \leq \dot{\theta}_{\max} \quad \text{for } i = 1..N_c \\ \tilde{v}_{\min} \leq \tilde{v}(k+i) \leq \tilde{v}_{\max} \quad \text{for } i = 1..N_c \\ \tilde{X}(0) = \tilde{X}(k) \\ \tilde{X}(k+i+1) = A\tilde{X}(k+i) + B\tilde{v}(k+i) \quad \text{for } k \geq 0 \\ \tilde{y}(k+i) = C\tilde{X}(k+i) \quad \text{for } k \geq 0 \end{array} \right.$$

- ✓ Iterating the discrete dynamics over the prediction horizon gives:

$$\begin{pmatrix} \tilde{X}(k+1) \\ \tilde{X}(k+2) \\ \vdots \\ \tilde{X}(k+N) \end{pmatrix} = \begin{pmatrix} A \\ A^2 \\ \vdots \\ A^N \end{pmatrix} \tilde{X}(k) + \begin{pmatrix} B & 0 & \cdots & 0 \\ AB & B & \ddots & \vdots \\ \vdots & \ddots & \ddots & 0 \\ A^{N-1}B & \cdots & AB & B \end{pmatrix} \begin{pmatrix} \tilde{v}(k) \\ \tilde{v}(k+1) \\ \vdots \\ \tilde{v}(k+N-1) \end{pmatrix}$$



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## Proposed MPC controller

Model (ii)  
Predictive  
Controller

- ✓ Let us now consider the following cost function:

$$V(k) = \sum_{i=0}^{N-1} (\| \tilde{X}(k+i) \|_Q^2 + \| \tilde{v}(k+i) \|_R^2) + \tilde{X}(k+N)^T Q_f(N) \tilde{X}(k+N)$$

- ✓ Which can be rewritten in the following compact form:

$$V(k) = \sum_{i=0}^{N-1} l(\tilde{X}(k+i), \tilde{v}(k+i)) + F(\tilde{X}(k+N))$$

- ✓ By substituting  $\tilde{X}(k+i) = A^i \tilde{X}(k) + \sum_{j=0}^{i-1} A^j B \tilde{v}_{k+i-1-j}$  in the previous costs yields:

$$\begin{cases} V(k) = \min \left( \frac{1}{2} \tilde{v}_{\rightarrow k}^T H \tilde{v}_{\rightarrow k} + \tilde{X}(k)^T F \tilde{v}_{\rightarrow k} \right. \\ \quad \left. + \frac{1}{2} \tilde{X}(k)^T Y \tilde{X}(k) \right. \\ \quad \left. \text{s.t } G \tilde{v}_{\rightarrow k} \leq W + E \tilde{X}(k) \right. \end{cases}$$

- ✓ The solution is obtained by zeroing  $\text{grad}_{\tilde{v}_{\rightarrow k}} V(k)$

## Nonlinear Disturbance observer

Nonlinear<sup>(iv)</sup>  
Disturbance  
Observer

- ✓ In typical rehabilitation scenarios, when the wearer is asked to develop a muscle activation, the human torque is considered an external disturbance
- ✓ We propose an NDO to estimate its values
- ✓ The dynamics of the system can be rewritten as follows:

$$\dot{X} = F_1(X) + G_1(X)\tau_e + G_2(X)d$$

✓ Where:

$$G_1(X) = G_2(X) = \begin{pmatrix} 0 \\ \frac{1}{J} \end{pmatrix}$$

- ✓ The proposed nonlinear observer is designed as follows:

$$\begin{cases} \hat{d} = z + p(X) \\ \dot{z} = L(-F_1(X) - G_1(X)\tau_e - G_2(X)(z + p(X))) \end{cases}$$

- ✓ Where:

$$\hat{d} = \hat{\tau}_h, p(X) = k_1\theta + k_2\dot{\theta}, L = \frac{\partial p(X)}{\partial X} = (k_1 \ k_2)$$

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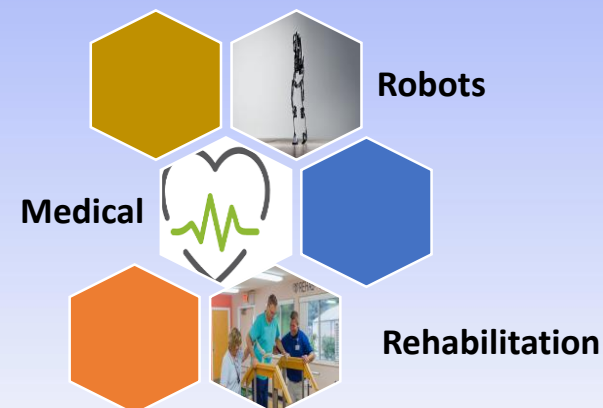
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# Experimental results

## MPC



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Speaker : **A. CHEMORI**



Video of the real-time experiments of the paper



## An Assistive Explicit Model Predictive Control Framework for a Knee Rehabilitation Exoskeleton

Submitted to : IEEE/ASME Transactions On Mechatronics

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[Jammeli et al 2021] I. Jammeli, A. Chemori, H. Moon, S. Elloumi and S. Mohammed, "An Assistive Explicit Model Predictive Control Framework for a Knee Rehabilitation Exoskeleton", IEEE/ASME Transactions on Mechatronics, DOI: 10.1109/TMECH.2021.3126674, 2021.



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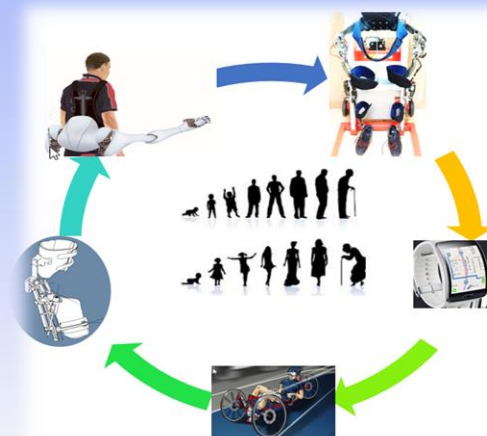
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## Problem

- Control of wearable robotic devices
- Those mechanical frames designed to be worn by humans
- For : **Civilian, work/industry, medical, military applications**

## Challenges

- ✗ Deal with complex structures
- ✗ Uncertainties, nonlinearities, friction, ...
- ✗ Interaction with the wearer (human)
- ✗ Safety aspects

## Solutions

- ✓ Different advanced control schemes (linear and nonlinear)
- ✓ L1 Adaptive, MPC-Based control schemes

## Validations

- ✓ Validation in simulation (different scenarios)
- ✓ Real-time experiments → EICOSI exoskeleton
- ✓ Rehabilitation applications

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